

IONIC EQUILIBRIUM



In this chapter, we'll study about equilibrium of weak electrolytes.

There are 2 types of substances.

Non electrolyte - which does not ionise in their aqueous solution.
e.g:- urea, glucose, sucrose etc.

Electrolyte - which will dissociate into ions in their aqueous solution.

ELECTROLYTES

Strong
Electrolytes

Completely dissociate
into ions

$$\alpha = 1$$

e.g:- HCl , H_2SO_4 , etc

Weak
Electrolytes

Partially dissociate
into ions

$$\alpha < 1$$

e.g:- CH_3COOH , NH_3 , etc

We will frequently use an operator in this chapter $\equiv P$

$$P \equiv -\log$$

l.g:- $-\log [H^+] = p^H$
 $-\log [K_a] = pK_a$

$-\log [OH] = p^{OH}$
 $-\log [K_b] = pK_b$

BASICS OF LOGARITHM

$\log m^n = n \log m$

$\log \frac{m}{n} = \log m - \log n$

$\ln x = (\log x) 2.303$

$\log 10 = 1$

$\log \frac{1}{x} = -\log x$

$\log m^n = \log m + \log n$

$\log_a m = \frac{\log_b m}{\log_b a}$

$\log 1 = 0$

$\log 2 = 0.3$

$\log 3 = 0.48$

if $\log_a x = \gamma$
 antilog $x = a^\gamma$

QUESTION

Calculate the following

1. $\log 25$

2. $\log 1.8$

3. $\log \frac{21}{7}$

4. $\log 5$

5. $\log \frac{22}{3}$

Solution

1. $\log 25 = \log (5)^2 = 2 (\log \frac{10}{2})$

$2 [\log 10 - \log 2]$

$2 [1 - 0.3] = 2(0.7) = 1.4$

$$\begin{aligned}
 2. \log 1.8 &= \log \frac{18}{10} = \log 18 - \log 10 \\
 &= \log 3^2 \times 2 - 1 \\
 &= 2(0.48) + 0.3 - 1 \\
 &= 0.96 + 0.3 - 1 = 1.26 - 1 \Rightarrow 0.26
 \end{aligned}$$

$$3. \log \frac{21}{7} = \log 3 \Rightarrow 0.48$$

$$4. \log 5 = \log \frac{10}{2} = 1 - 0.3 \Rightarrow 0.7$$

$$\begin{aligned}
 5. \log \frac{22}{3} &= \log 22 - \log 3 \\
 &= \log 2 + \log 11 - 0.48 \\
 &= 0.3 + \frac{\log 10 + \log 12}{2} - 0.48 \\
 &= -0.18 + \\
 &\Rightarrow 0.86
 \end{aligned}$$

Que:-

1. $\log 1.8 \times 10^{-5}$
2. $\log 14 \times 10^{-6}$
3. $\log 7 \times 10^{-5}$

Ans:-

1. $\log 1.8 \times 10^{-5} = 0.26 - 5 = -4.74$
2. $\log 14 - 6 = \log 7 + 0.3 - 6$
 $= 0.84 + 0.3 - 6$
 $= 1.14 - 6 \Rightarrow -4.86$
3. $\log 7 \times 10^{-5} = \log(7-5) = 0.84 - 5$
 $\Rightarrow -4.16$

REMEMBER

$\log 1.8 = 0.26$
 $\log 7 = 0.84$
 $\log 5 = 0.7$
 $\log 2 = 0.3$
 $\log 3 = 0.48$



3. LEWIS THEORY

Lone pair donors are **base**.

Lone pair acceptors are **acids**.



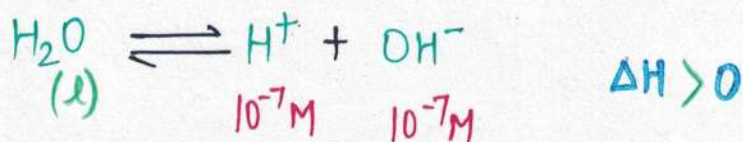
➤ According to first two theories, water is a neutral solution but according to third theory H_2O is Lewis base.

PROPERTIES OF WATER

① It is a Neutral Solution.

② It is a pure liquid having concentration = $\frac{1000}{18} = 55.55 \text{ M} = 55.55 \text{ M}$

③ At 25°C H_2O dissociates into H^+ and OH^- ion having concentration 10^{-7} M each.



④ $K_w =$ ionic product of water

$$K_w = [\text{H}^+][\text{OH}^-]$$

taking log on both sides

$$-\log K_w = -\log [\text{H}^+][\text{OH}^-]$$

$$pK_w = -\log [\text{H}^+] - \log [\text{OH}^-]$$

$$pK_w = p\text{H} + p\text{OH}$$

at 25°C $pK_w = p\text{H} + p\text{OH} = 14$

We can predict the nature of solution by pH or pOH

a. $[H^+] = [OH^-]$ Natural solution

$$-\log[H^+] = -\log[OH^-]$$

$$pH + pOH = pOH + pH$$

$$2pH = 14$$

$$pH = 7$$

b. $[H^+] > [OH^-]$ Acidic solution

$$-\log[H^+] < -\log[OH^-]$$

$$pH + pOH < pOH + pH$$

$$2pH < 14$$

$$pH < 7$$

$[H^+] < [OH^-]$ Basic solution

$$-\log[H^+] > -\log[OH^-]$$

$$pH + pOH > pOH + pH$$

$$2pH > 14$$

$$pH > 7$$

pH Scale





Q.ve. Predict the nature of solnⁿ by looking at pH values if at 90°C
 $K_w = 10^{-13}$ for water.

a. $pH = 7$

b. $pH = 6$

c. $pH = 6.5$

d. $pH = 8$

Soluⁿ:- $pK_w = pH + pOH \Rightarrow 13$

Neutral solnⁿ if $[H^+] = [OH^-]$

$$2pH = pH + pOH$$

$$pH = \frac{13}{2} = 6.5$$

acidic solnⁿ if $pH < 6.5$

basic solnⁿ if $pH > 6.5$

So now, @ $pH > 6.5 \Rightarrow$ basic solnⁿ

$pH = 6$ (b) $pH < 6.5 \Rightarrow$ Neutral solnⁿ

(c) $pH = 6.5 \Rightarrow$ Neutral solnⁿ

$pH = 8$ (d) $pH > 6.5 \Rightarrow$ basic solnⁿ



Q. What will be effect on pH and pOH of solution if temperature will increase?

Soluⁿ:- On increasing temperature, K_w will increase hence, both $[H^+]$ and $[OH^-]$ if increase, so pH and pOH will both decrease.

5. Degree of Dissociation of H_2O at 25°C



$t = 0$ c

$t = t$ $c-x$ x x

$$\alpha = \frac{x}{c}$$

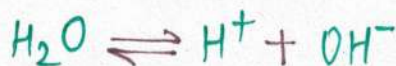
$$\alpha = \frac{10^{-7}}{\frac{1000}{18}} = 1.8 \times 10^{-9}$$

$$\% \alpha = 1.8 \times 10^{-7}$$

ABSOLUTE DISSOCIATION CONSTANT

OR

IONISATION CONSTANT FOR WATER



K_a = dissociation constant for weak acid

K_b = dissociation constant for weak base

$$\text{at } 25^\circ\text{C} \quad K_a = K_b = \frac{[\text{H}^+][\text{OH}^-]}{[\text{H}_2\text{O}]}$$

$$= \frac{10^{-7} \times 10^{-7}}{\frac{1000}{18}} = 1.8 \times 10^{-16}$$

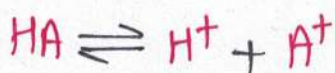
$$\| -\log K_a = -\log K_b = -\log 1.8 \times 10^{-16} \|\|$$

$$pK_a = pK_b = -[0.26 - 16.00]$$

$$pK_a = pK_b = -[-15.74]$$

$$pK_a = pK_b = 15.74$$

On increasing temperature K_a K_b will increase pK_a , pK_b will decrease.



$$K_a = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]}$$



$$K_b = \frac{[\text{HA}][\text{OH}^-]}{[\text{A}^-]}$$

$$K_a K_b = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]} \cdot \frac{[\text{HA}][\text{OH}^-]}{[\text{A}^-]} \Rightarrow K_a K_b = [\text{H}^+][\text{OH}^-]$$

$$K_a K_b = 10^{-14}$$



$$\| -\log K_a - \log K_b = -\log 10^{-14} \|$$

$$pK_a + pK_b = 14$$

$$K_a K_b = \text{Constant} = 10^{-14}$$

$\therefore K_a K_b$ is constant, if acid is strong, then its conjugate base should be weak.

PH Calculation

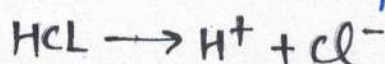
Calculate pH of :-

1. 300 ml 0.1 M HCL

$$[H^+] = \frac{0.1}{300} \times 1000$$

$$-\log\left(\frac{1}{3}\right) = \log 3$$

$$pH = 0.48$$



$$[H^+] = 0.1 M$$

$$pH = -\log 0.1 \quad \boxed{pH = 1}$$

$$300 \text{ ml} = 0.1$$

$$1000 \text{ ml} = \frac{0.1}{300} \times 1000$$

$$= \frac{1}{3} N$$

2. 500 ml 0.1 M HCl

$$\boxed{pH = 1}$$

3. 300 ml 0.2 M HCl + 200 ml 0.4 M H₂SO₄

$$[H^+] \text{ from HCl} = 0.2$$

$$[H^+] \text{ from H}_2\text{SO}_4 = 0.8$$

$$\text{total } [H^+] = 1$$

$$-\log [H^+] = -\log 1$$

$$\text{millimole of } H^+ \text{ from HCl} = 300 \times 0.2 = 60$$

$$H^+ \text{ from H}_2\text{SO}_4 = 0.8 \times 200 = 160$$

$$\log 11 = \frac{\log 12 + \log 10}{2}$$

$$= \frac{2(0.3) + 0.48 + 1}{2}$$

$$\log \frac{22}{5} = \frac{1.08 + 1}{2} \Rightarrow \frac{2.08}{2}$$

$$- \log 5$$

$$= 0.3 + 1.04 - [1 - 0.3]$$

$$= 1.34 - (0.7)$$

$$= 0.64$$

$$\text{Total} = 160 + 60 = 220 \text{ millimole}$$

$$[H^+] = \frac{220}{500} = \frac{22}{50}$$

$$= -\log \frac{22}{50}$$

$$= -\left[\log \frac{22}{50} - \log 10\right]$$

$$= -\left[\log \frac{22}{5} - 1\right]$$

$$= -(0.64 - 1)$$

$$\text{PH} = 0.36$$

$$\text{PH} = 0.36$$

▷ 300 ml 0.2 M H₂SO₄ + 300 ml 0.2 M HCl + 200 ml 0.2 M HNO₃

$$\text{mill. from H}_2\text{SO}_4 = 0.2 \times 300 \times 2$$

$$= 120$$

$$\text{from HCl} = 0.2 \times 300 = 60$$

$$\text{from HNO}_3 = 0.2 \times 200 = 40$$

$$\text{Total} = [H^+] = \frac{120 + 60 + 40}{800} = \frac{220}{800}$$

$$\log 11 + \log 2$$

$$= \log 11 \times 2$$

$$\log 22 = 1.34$$

$$-\log [H^+] = -\log \left(\frac{22}{800}\right)$$

$$= -[\log 22 + \log 11 - \log 8 - 1]$$

$$= -[1.34 - 0.9 - 1]$$

$$= -[0.44 - 1]$$

$$= 0.56$$

4. 300 ml 0.1 M NaOH

$$[H^+] = 0 \quad \text{pOH} = 1$$

$$\text{pH} = 14 - 1$$

$$\text{pH} = 13$$

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5. 300 ml 0.2M NaOH + 200 ml 0.2M Ca(OH)₂

$$[\text{OH}^-] = \frac{60+80}{500} = \frac{140}{500}$$

$$-\log [\text{OH}^-] = -\log \left[\frac{14}{50} \right]$$

$$= - \left[+\log 7 + \log 2 - 2 \log 5 - \log 2 \right]$$

$$- (.84 + 0.3 - 2(1 - 0.3) - 0.3)$$

$$- (.84 - 1.4)$$

$$= 0.56 \Rightarrow \text{pH} = 14 - 0.56 \Rightarrow 13.44$$

$$\boxed{\text{pH} = 13.44}$$

6. 300 ml 0.2M Ca(OH)₂ + 200 ml 0.2M NaOH + 300 ml 0.1M

$$[\text{OH}^-] = \frac{120+40+90}{800} = \frac{250}{800}$$

Al(OH)₃

$$\text{pOH} = -\log \frac{25}{80}$$

$$= - \left[2 \log 5 - 3 \log 2 \right]$$

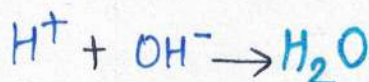
$$= - \left[2(0.7) - 3(0.3) \right]$$

$$= - \left[1.4 - 0.9 \right] = 0.5$$

$$\text{pH} = 14 - 0.5 \Rightarrow 13.5$$

$$\boxed{\text{pH} = 13.5}$$

Acid + Base \longrightarrow Salt + Water



millimole of H⁺ = millimole of OH⁻ \longrightarrow neutral
 millimole of H⁺ > millimole of OH⁻ \longrightarrow acidic
 millimole of H⁺ < millimole of OH⁻ \longrightarrow basic

Ques:- 300 ml 0.2M NaOH + 200 ml 0.3M HCL

$$\text{millimole } [\text{OH}^-] = 0.2 \times 300 = 60$$

$$\text{millimole } [\text{H}^+] = 0.3 \times 200 = 60$$

$$\text{millimole } [\text{H}^+] = \text{millimole } \text{OH}^-$$

$$\boxed{\text{pH} = 7}$$

Ques:- 300 ml 0.3M HCL + 200 ml 0.2M NaOH

$$\text{millimole } \text{H}^+ = 90$$

$$\text{OH}^- = 40$$

$$K_w = [\text{OH}^-][\text{H}^+] = 0.06 \quad \text{H}^+ > \text{OH}^- \quad \text{pH } \text{H}^+ = \frac{56}{500} \text{ millimole.}$$

$$\text{pH} = -\log \frac{6}{100} = -(0.78 - 2) \text{ acidic}$$

$$\text{pH} = 1 \quad \frac{1}{10}$$

Ques:- 300 ml 0.2M HCL + 200 ml 0.5M NaOH

$$\text{milli } \text{H}^+ = 60$$

$$\text{milli } \text{OH}^- = 100$$

$$\text{OH}^- > \text{H}^+$$

$$\text{basic } \text{pH} > 7$$

$$\text{pH} = 1.1$$

$$\boxed{\text{pH} = 12.9}$$

Ques:- what is the pH of resulting solun if pH=2 and pH=4 are added in following volume ratio:-

a. 1:1

b. 2:3

c. 3:2

Solun:- $2 = -\log \text{H}^+$

$$10^{-2} = [\text{H}^+] \quad [\text{OH}^-] = 10^{-12}$$

$$10^{-2} = \frac{n_1}{V_1}$$

$$4 = -\log \text{H}^+$$

$$10^{-4} = [\text{H}^+]$$

$$10^{-10} = [\text{OH}^-]$$

$$10^{-4} = \frac{H_2}{V_2}$$

$$n_1 : H_2 = \frac{10^{-2}}{10^{-4}} = 10^2$$

$$V_2 = \frac{H_2}{10^{-4}}$$

$$[\text{H}^+] = \frac{n_1 + n_2}{\frac{2n_2}{10^{-4}}} = \frac{10^2 n_2 + n_2}{\frac{2n_2}{10^{-4}}} = \frac{10/n_2}{2n_2/10^{-4}}$$

$$[H^+] = \frac{101 \times 10^{-4}}{2}$$

$$-pH = -(\log 101 - 4 - 0.3)$$
$$= -(2 - 4.3)$$

$$pH = 2.3$$

2:3

$$n_1 : n_2 = \frac{n_1 + n_2}{2n_2} \quad 2:3$$

$$\frac{V_1}{V_2} = \frac{2}{3}$$

$$\frac{n_1}{10^{-2}} \times 10^{-4-2} = \frac{2}{3}$$

$$\frac{n_1}{V_1} = 10^{-2}$$

$$\frac{n_1}{n_2} = \frac{2}{3} \times 10^2 = \frac{200}{3}$$

$$n_1 = \frac{200}{3} n_2$$

$$[H^+] = \frac{10^{-2}V_1 + 10^{-4}V_2}{5V_1 + V_2}$$

$$[H^+] = \frac{2V \times 10^{-2} + 3V \times 10^{-4}}{2V + 3V}$$

$$= \frac{2 \times 10^{-2} + 3 \times 10^{-4}}{5}$$

$$[H^+] = \frac{0.02}{10} + \frac{0.0003}{5} = \frac{0.0203}{5}$$

$$= -\log \left(\frac{0.0205}{5} \right)$$

$$= -\left(\log \frac{2050}{10000} - 0.7 \right)$$

$$= -\left(\log 200 - 4 - 0.7 \right)$$

$$= -\left(\log 2 + 2 - 4.7 \right)$$

$$= -(2.3 - 4.7)$$

$$pH = 2.4$$



$$3V \ 10^{-2} H$$

$$2V \ 10^{-4}$$

$$\begin{aligned} [H^+] &= \frac{0.03 + 0.0002}{5} \\ &= \frac{0.0302}{5} \approx \frac{0.0300}{5} \\ &= -\log \left(\frac{0.03}{5} \right) \\ &= -(\log 3 - 2 - 0.7) \\ &= -(0.48 - 2.70) \\ &= -(-2.22) \\ &= 2.22 \end{aligned}$$

Ques:- $pH = 12$ $pH = 10$

$$[H^+] = 10^{-12} \quad [H^+] = 10^{-10}$$

(i) $V \ 10^{-12} M$ $V \ 10^{-10} M$

$$[H^+] = \frac{10^{-12} + 10^{-10}}{2} = \frac{0.01 \times 10^{-10} + 10^{-10}}{2}$$

$$[H^+] = \frac{1.01 \times 10^{-10}}{2}$$

$$pH^+ = (10 - 0.3)$$

$$= -(9.7)$$

$$\boxed{pH^+ = 9.7}$$

$$pOH = 2$$

$$pOH = 4$$

$$[OH^-] = 10^{-2}$$

$$[OH] = 10^{-4}$$

(ii) $2V \ 10^{-2} M$ $3V \ 10^{-4}$

$$[OH^-] = \frac{0.02 + 0.0003}{5} = \frac{0.0200}{5}$$

$$pOH = 2.4$$

$$pH = 14 - 2.4 = 11.6$$



$$(iii) \text{ pH} = 2.2$$

$$\text{pOH} = 14 - 2.22 = 11.78$$

Ans: - $\text{pH} = 12$

$$\text{pH} = 2$$

$$\text{pOH} = 2$$

$$\text{pH} = 2$$

$$[\text{OH}^-] = 10^{-2}$$

$$[\text{H}^+] = 10^{-2}$$

$$[\text{H}^+] = 10^{-12}$$

➤ $2V \ 10^{-12} M$

$3V \ 10^{-2} M$

$$[\text{H}^+] = \frac{2 \times 10^{-12} + 3 \times 10^{-2}}{5}$$

$$= \frac{2 \times 0.00 \dots + 0.03}{5} \approx \frac{0.03}{5}$$

$$\text{pH} = \left[-\log \frac{0.03}{5} \right] = -(0.48 - 2 - 0.7)$$
$$= -(-2 - 0.7) + 0.48$$

$$[\text{OH}^-] = 10^{-2}$$

$$[\text{H}^+] = 10^{-2}$$

$$10^{-2} = \frac{\eta}{V_1}$$

$$10^{-2} = \frac{\eta}{V_2}$$

$$10^{-2} = \frac{3\eta}{2V_2}$$

$$10^{-2} = \frac{\eta}{V_2}$$

$$\eta = \frac{2V_2}{3} \times 10^{-2}$$

$$\eta = V_2 \times 10^{-2}$$

millimole (OH^-) millimole $[\text{H}^+] \rightarrow \text{H}_2\text{O}$

$$3V \times 10^{-2} \quad \color{red}{\blacklozenge} \quad 2V \times 10^{-2}$$

$$[\text{OH}^-] \ V \times 10^{-2}$$

$$[\text{OH}^-] = \frac{10^{-2}}{5} \Rightarrow -\log \left(\frac{10^{-2}}{5} \right)$$

$$\Rightarrow -(-2 - 0.7)$$

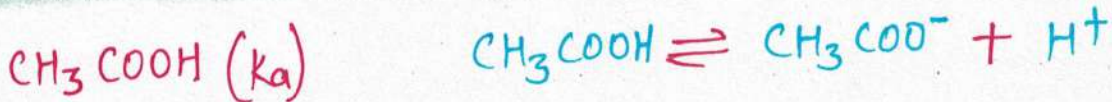
$$\text{pH} = 14 - 2.7 \Rightarrow 11.3$$

$$\triangleright 3\sqrt{10^{-2} M H^+} \quad 2\sqrt{10^{-2} M H^+}$$

$$H^+ = \sqrt{10^{-2}} \quad [H^+] = \frac{10^{-2}}{5}$$

$$\boxed{pH = 2.7}$$

pH Calculation for Weak Acid



$$\begin{array}{cccc} t=0 & c & & \\ t=t & c(1-\alpha) & c\alpha & c\alpha \end{array}$$

$$K_a = \frac{c\alpha^2}{1-\alpha}$$

$$1-\alpha \approx 1 \quad \alpha = \sqrt{\frac{K_a}{c}}$$

$$[H^+] = c\alpha = c\sqrt{\frac{K_a}{c}} = \sqrt{cK_a}$$

$$-\log [H^+] = pH = -\frac{1}{2} (\log c + \log K_a)$$

$$\boxed{pH = \frac{1}{2} (pK_a - \log c)}$$

Ques:- What is pH of 0.1 M CH_3COOH ($K_a = 1.8 \times 10^{-5}$)



$$\begin{array}{cccc} t=0 & 0.1 & & \\ t=t & 0.1(1-\alpha) & 0.1\alpha & 0.1\alpha \end{array}$$

$$K_a = \frac{c\alpha^2}{1-\alpha} \Rightarrow 1.8 \times 10^{-5} = \alpha^2 \times 0.1$$

$$\alpha = \sqrt{1.8 \times 10^{-5} \times 10}$$

$$\alpha = \sqrt{1.8 \times 10^{-4}}$$

$$\alpha = \sqrt{1.8 \times 10^{-2}}$$

$$pH = -\frac{1}{2} (0.26 - 6)$$

$$pH = -\frac{1}{2} (-5.74) \Rightarrow 2.87$$

$$\% \alpha = \sqrt{1.8 \times 10^{-2}} \times 100$$

$$\sqrt{1.8\%} = 1.34\%$$

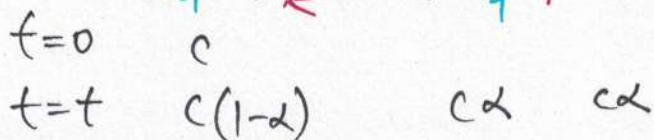
if $K_a < 10^{-3}$, then it is weak acid.

pH Calculation for Weak Base

NH_3 or NH_4OH (K_b)



or



$$K_b = \frac{[\text{OH}^-][\text{NH}_4^+]}{[\text{NH}_4\text{OH}]}$$

$$K_b = \frac{(c\alpha)(c\alpha)}{c(1-\alpha)} = \frac{c\alpha^2}{1-\alpha}$$

$$1-\alpha \approx 1$$

$$K_b = c\alpha^2$$

$$\alpha = \sqrt{\frac{K_b}{c}}$$

$$[\text{OH}^-] = c\alpha = c\sqrt{\frac{K_b}{c}} \Rightarrow \sqrt{cK_b}$$

$$\begin{aligned} -\log[\text{OH}^-] &= pK_b = -\frac{1}{2}(\log c + \log K_b) \\ &= \frac{1}{2}(\log K_b - \log c) \end{aligned}$$

Que:- What is pH of 0.1 M NH_3 ($K_b = 1.8 \times 10^{-5}$)



0.1



$$K_b = \frac{x^2}{0.1-x}$$

$$x = \sqrt{K_b \times 0.1}$$

$$x = \sqrt{1.8 \times 10^{-6}}$$

$$x = \sqrt{1.8 \times 10^{-3}}$$

$$pK_b = \frac{1}{2} (\log 1.8 \times 10^{-5} - \log 0.1)$$

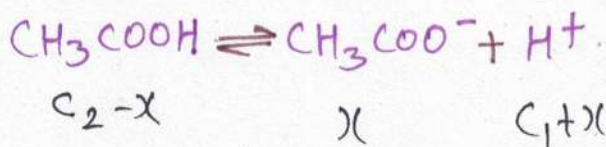
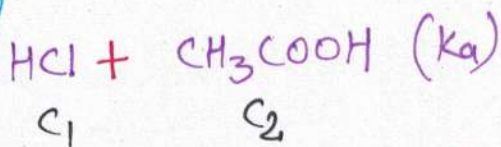
$$pH = -\frac{1}{2} \left[\frac{2.6}{2} - 3 \right] = 3 - 0.13 = 2.87$$

$$pK_b = \frac{1}{2} [0.26 - 5 + 1]$$

$$= \frac{1}{2} [51.74] \Rightarrow 2.87$$

$$pH = 14 - 2.87 \Rightarrow 11.13$$

— Strong acid + Weak acid —



$$K_a = \frac{x(c_1 + x)^0}{c_2 - x^0}$$

$$x = \frac{c_2 K_a}{c_1}$$

$$[H^+] = c_1 + x$$

$$= c_1$$

Ques:- $CH_3COOH + HCl$

$$K_a = 1.8 \times 10^{-5} \quad pH = ?$$

α CH_3COOH

$$1.8 \times 10^{-5} = \frac{c_1 x}{c_2}$$

$$x = 1.8 \times 10^{-5} \frac{c_2}{c_1}$$

$$\alpha = \frac{x}{c_2} = \frac{1.8 \times 10^{-5}}{0.1} \Rightarrow 1.8 \times 10^{-4}$$

$$\% \alpha = 1.8 \times 10^{-2} \%$$

$$[H^+] = 0.1$$

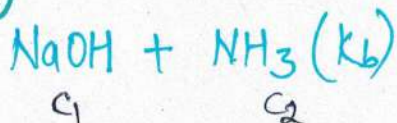
$$-\log H^+ = -\log 0.1$$

$$pH = 1$$

dissociation of CH_3COOH is decreased further due to common ion effect.

In a solnⁿ of strong acid and weak acid pH of solnⁿ will be generated by strong acid.

Strong base + Weak Base



c_1

c_2



$c_2 - x$

x

$c_1 + x$

$$K_b = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]}$$

$$K_b = \frac{x(c_1 + x)}{c_2 - x}$$

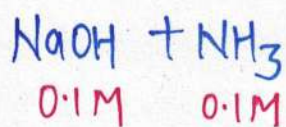
$$x = \frac{c_2 K_b}{c_1}$$

$$\alpha \text{NH}_3 = \frac{x}{c_2}$$

$$[\text{OH}^-] = c_1 + x$$

$$[\text{OH}^-] + c_1$$

Ques:-



0.1M

0.1M

$$[K_b = 1.8 \times 10^{-5}]$$

$$[\text{OH}^-] = 0.1$$

$$\text{pOH} = 1$$

$$\text{pH} = 13$$

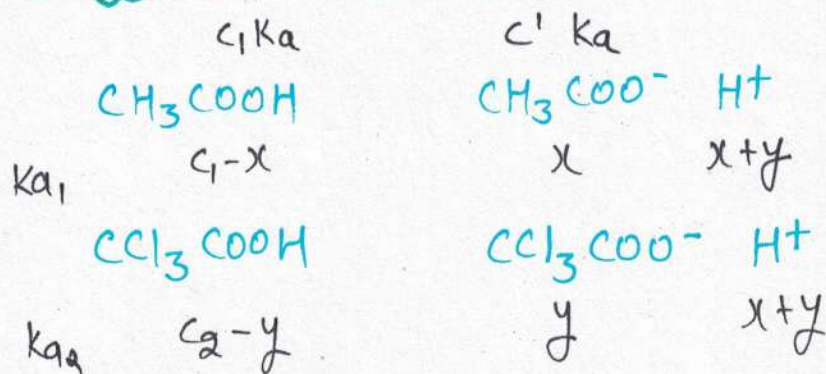
$$x = \frac{c_2 K_b}{c_1} = 0.1 \left(\frac{1.8 \times 10^{-5}}{0.1} \right)$$

$$\alpha = \frac{1.8 \times 10^{-5}}{0.1} = 1.8 \times 10^{-4}$$

$$\% \alpha = 1.8 \times 10^{-2} \%$$

pH for strong base + weak base will be governed by strong base.

Weak Base + Weak Acid



$$K_{a1} = \frac{x(x+y)}{c_1 - x} \Rightarrow c_1 K_{a1} = x(x+y)$$

$$K_{a2} = \frac{y(x+y)}{c_2 - y} \Rightarrow c_2 K_{a2} = (x+y)y$$

$$c_1 K_{a1} + c_2 K_{a2} = (x+y)(x+y)$$

$$(x+y) = \sqrt{c_1 K_{a1} + c_2 K_{a2}}$$

$$[\text{CH}_3\text{COO}^-] = x = \frac{c_1 K_{a1}}{x+y}$$

$$x = \frac{c_1 K_{a1}}{\sqrt{c_1 K_{a1} + c_2 K_{a2}}}$$

$$\alpha_{\text{CH}_3\text{COOH}} = \frac{y}{c_1}$$

$$[\text{CCl}_3\text{COO}^-] = y = \frac{c_2 K_{a2}}{x+y}$$

$$y = \frac{c_2 K_{a2}}{\sqrt{c_1 K_{a1} + c_2 K_{a2}}}$$

$$\alpha_{\text{CCl}_3\text{COOH}} = \frac{y}{c_2}$$

Ques



0.1M $K_a = 7 \times 10^{-5}$ 0.1M $K_a = 2 \times 10^{-5}$

(i) $[\text{H}^+] = \sqrt{0.1 \times 7 \times 10^{-5} + 0.1 \times 2 \times 10^{-5}}$

$$\sqrt{(7+2) \times 10^{-6}} = 3 \times 10^{-3}$$

$$-\log [\text{H}^+] = \text{pH} = -\log (3 \times 10^{-3})$$

$$\text{pH} = -[0.48 - 3]$$

$$\text{pH} = 2.52$$

$$(i) [CH_3COO^-] = \frac{C_2 K_{a2}}{x+y} = \frac{0.1 \times 2 \times 10^{-5}}{3 \times 10^{-3}}$$

$$= 0.66 \times 10^{-3}$$

$$[CCl_3COO^-] = \frac{0.1 \times 7 \times 10^{-5}}{3 \times 10^{-3}} = 2.33 \times 10^{-3}$$

$$(ii) \alpha_{CH_3COOH} = \frac{x}{c_1} = \frac{0.66 \times 10^{-3}}{0.10}$$

$$= 6.6 \times 10^{-3}$$

$$\% \alpha = 0.66\%$$

$$\alpha_{CCl_3COOH} = 23.3 \times 10^{-3}$$

$$\frac{y}{c_2} = 23.3 \times 10^{-3}$$

$$\% \alpha = 2.33\%$$

Q. 200ml 0.1M HCl + 300ml 0.2M H₂SO₄ + 300ml 0.2M CH₃COOH (K_a = 2 × 10⁻⁵)

$$[H^+] = \frac{20 + 60 \times 2}{800} = \frac{140}{800}$$

$$-\log H^+ = pH = -\log \frac{14}{80}$$

$$= -[\log 7 + 0.3 - \log 80]$$

$$= -[1.13 - (1.9)]$$

$$= [-0.77] = 0.77$$

$$\% \alpha_{CH_3COOH} = \frac{x}{c} = \frac{0.2 \times 2 \times 10^{-5}}{0.3} = \frac{0.4 \times 10^{-3}}{0.3}$$



0.2

0.2-x

x

x

$$x = \sqrt{c K_a}$$

$$x = \sqrt{0.2 \times 2 \times 10^{-5}} = 2 \times 10^{-5}$$

$$= 1.33 \times 10^{-3} \times 100$$

$$= 1.33 \times 10^{-1}$$

$$= 0.133\%$$



$$\frac{60}{800} - x \qquad x \qquad \frac{140}{800} + x$$

$$K_a = \frac{\frac{140}{800} x}{\frac{60}{800}}$$

$$x = \frac{2 \times 10^{-5} \times 6}{14}$$

$$x = \frac{6}{7} \times 10^{-5}$$

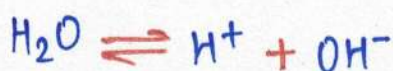
$$\% \alpha_{\text{CH}_3\text{COOH}} = \frac{x}{\frac{60}{800}} \times 100$$

$$= \frac{6}{7} \times \frac{10^{-5}}{60} \times 8 \Rightarrow \frac{8}{7} \times 10^{-5}$$

DILUTION



$$0.1\text{M} \qquad 0.1$$



$$0.1+x \qquad x$$

$$(0.1+x)x = 10^{-14}$$

$$x = 10^{-13}$$

$$[\text{H}^+] = 0.1 + 10^{-13}$$

$$-\log[\text{H}^+] = \boxed{\text{pH} = 1}$$

$$\alpha_{\text{H}_2\text{O}} = \frac{x}{c} = \frac{10^{-13}}{\frac{1000}{18}} \approx 1.8 \times 10^{-15}$$



$$10^{-2} \qquad 10^{-2}$$



$$10^{-2}+x \qquad x$$

$$(10^{-2}+x)x = 10^{-14}$$

$$x = 10^{-12}$$

$$[\text{H}^+] = 10^{-2} + 10^{-12}$$

$$\boxed{\text{pH} = 1}$$

$$\alpha_{\text{H}_2\text{O}} = \frac{10^{-12}}{\frac{1000}{18}} = 1.8 \times 10^{-14}$$



$$10^{-8} \text{M} \quad 10^{-8} \text{M}$$



$$10^{-8} + x \quad x$$

$$x(10^{-8} + x) = 10^{-14}$$

$$x^2 + 10^{-8}x - 10^{-14} = 0$$

$$x = \frac{-10^{-8} + \sqrt{10^{-16} + 4 \times 10^{-14}}}{2}$$

$$x = \frac{-10^{-8} + 10^{-8} \sqrt{401}}{2}$$

$$x = \frac{19}{2} \times 10^{-8}$$

$$[\text{H}^+] = 10^{-8} + \frac{19}{2} \times 10^{-8}$$

$$= \frac{21}{2} \times 10^{-8}$$

$$\text{pH} = -\log\left(\frac{21}{2} \times 10^{-8}\right)$$

$$\text{pH} = -[\log 21 - 0.3 - 8]$$

$$\text{pH} = -[0.7 + 0.6 - 8.3]$$

$$\text{pH} = 7$$

$$\boxed{\text{pH} = 6.98}$$



pH of 10^{-8}M NaOH



$$10^{-8} \quad 10^{-8}$$



$$x \quad 10^{-8} + x$$

$$(10^{-8} + x)x = 10^{-14}$$

$$x = \frac{19}{2} \times 10^{-8}$$

$$[\text{OH}^-] = 10^{-8} + \frac{19}{2} \times 10^{-8}$$

$$\text{pOH} = 6.98$$

$$\text{pH} = 14 - 6.98 = 7.02$$

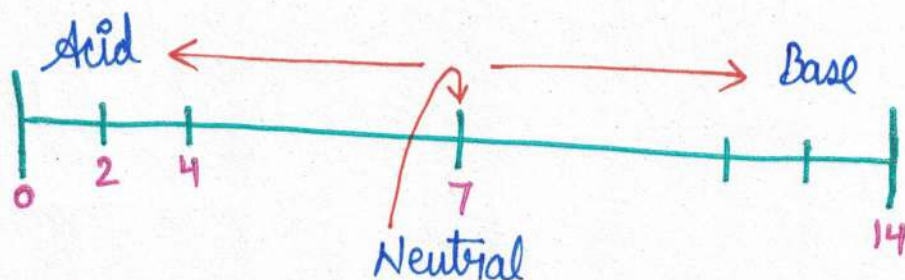
$$\boxed{\text{pH} = 7.02}$$



$$\begin{aligned}
 -\log [H^+] &= -\log \left[\frac{19}{2} \times 10^{-8} \right] \\
 &= -[\log 19 + 0.3 - 8] \\
 &= \frac{0.48 \times 2 + 0.3 + 1.3}{2} \\
 &= \frac{0.96 + 1.6}{2} \\
 &= \frac{2.56}{2} \Rightarrow 1.28
 \end{aligned}$$

$$pH = 8.3 - 1.28$$

$$pH = 7.02$$



If $[H^+] < 10^{-6} M$ Then consider water equilibrium catalyst are substances which can affect the rate of reaction. It cannot disturb the equilibrium.

The amount of catalyst before and after the reaction will be constant.

SALT HYDROLYSIS

Salts are of 4 kinds:-

1. Salt of strong acid, strong base

After complete neutralisation of strong acid with strong base, we'll get these type of salt.

e.g:- NaCl, K_2SO_4 etc.

2. Salt of strong acid and weak base

After complete neutralisation of strong acid and weak base, we'll get these type of salts.

e.g.: NH_4Cl , $\text{CH}_3\text{NH}_3\text{Cl}$ etc.

3. Salt of strong base and weak acid

After complete neutralisation of weak acid and strong base, we'll get these type of salts.

e.g.: CH_3COONa ,  etc.

4. Salt of weak acid and weak base

After neutralisation of weak acid and weak base we'll get these type of salts.

e.g.: $\text{CH}_3\text{COONH}_4$, HCOONH_4 etc.

When salt is dissolved in water, the anion or cation which comes from weak acid or base will react with H_2O , the process is called spectator ion.

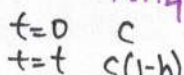
1. Strong Acid + Strong Base



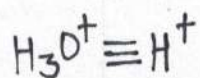
$$[\text{H}^+] = [\text{OH}^-] = 10^{-7}$$

$$\text{pH} = 7$$

2. Strong Acid + Weak Base



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$$K_h = \frac{[\text{NH}_3][\text{H}^+]}{[\text{NH}_4^+]} = \frac{ch^2}{1-h}$$

$$1-h \approx 1$$

$h \rightarrow$ degree of hydrolysis

$K_h \rightarrow$ hydrolysis constant

$$ch^2 = K_h$$

$$h = \sqrt{\frac{K_h}{c}}$$



$$K_b = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]} \frac{[\text{H}^+]}{[\text{H}^+]}$$

$$K_b = \frac{K_w}{K_h} \Rightarrow K_h = \frac{K_w}{K_b}$$

$$K_{b\text{NH}_3} K_{b\text{NH}_4^+} = 10^{-14} = K_w$$

$$[\text{H}^+] = ch = c \sqrt{\frac{K_h}{c}} = \sqrt{c K_h}$$

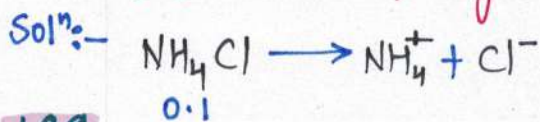
$$[\text{H}^+] = \sqrt{\frac{K_w}{K_b} c}$$

$$\begin{aligned} -\log [\text{H}^+] = \text{pH} &= -\frac{1}{2} (\log K_w + \log c - \log K_b) \\ &= -\frac{1}{2} (\log 10^{-14} + \log c - \log K_b) \end{aligned}$$

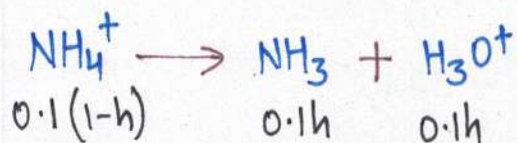
$$\text{pH} = 7 - \frac{1}{2} (\log c + \text{p}K_b)$$

$$\text{pH} < 7$$

QVE. What is the pH of 0.1M NH_4Cl solution given K_b of $\text{NH}_3 = 1.8 \times 10^{-5}$
also K_b of $\text{NH}_3 = 1.8 \times 10^{-5}$
also calculate % hydrolysis of NH_4Cl



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$$h = \sqrt{\frac{K_h}{0.1}}$$

$$K_h = \frac{K_w}{K_b} = \frac{10^{-14}}{1.8 \times 10^{-5}} = \frac{10^{-7}}{1.8}$$

$$h = \sqrt{\frac{10^{-9}}{1.8 \times 0.1}}$$

$$h = \sqrt{\frac{10^{-9}}{1.8}} = \frac{\sqrt{1.8}}{1.8} = 10^{-5}$$

$$\%h = \frac{\sqrt{1.8}}{1.8} \times 10^{-3}$$

$$-\log x = \log \sqrt{\frac{10^{-15}}{1.8 \times 10^{-5}}} = \log x$$

$= 5.13$

~~.....~~

$$pH = \frac{7-1}{2} (pK_b - 1)$$

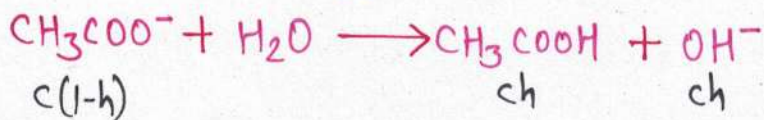
$$pH = 7 - \frac{1}{2} [5 - 0.26 - 1]$$

$$pH = 7 - \frac{1}{2} (3.74)$$

$$pH = 7 - 1.87$$

$pH = 5.13$

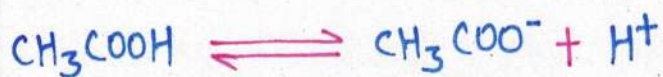
3. Weak Acid + Strong Base



$$K_h = \frac{ch^2}{1-h}$$

$h = \sqrt{\frac{K_h}{c}}$

$$1-h \approx 1$$



$$K_a = \frac{[\text{CH}_3\text{COO}^-][\text{H}^+]}{[\text{CH}_3\text{COOH}]} \quad \frac{[\text{OH}^+]}{[\text{OH}^-]}$$

$$K_a = \frac{K_w}{K_b}$$

$$K_b = \frac{K_w}{K_a}$$

$$[\text{OH}^-] = ch = c \sqrt{\frac{K_b}{c}} = \sqrt{cK_b}$$

$$p^{\text{OH}} = -\log [\text{OH}^-] = -\frac{1}{2} [\log c + \log K_w - \log K_a]$$

$$p^{\text{H}} = 14 + \frac{1}{2} (\log c - 14 + pK_a)$$

$$p^{\text{H}} = 7 + \frac{1}{2} (\log c + pK_a)$$

$$p^{\text{H}} > 7$$

basic solution

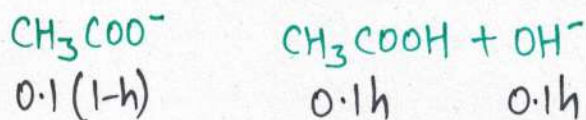
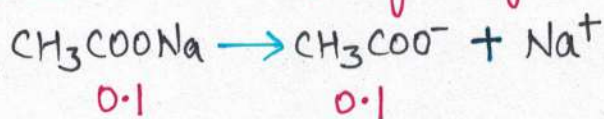


p^{H} of 0.1M $\text{CH}_3\text{COONa} = ?$

If K_a of $\text{CH}_3\text{COOH} = 1.8 \times 10^{-5}$

Also calculate % hydrolysis

Soluⁿ:-



$$K_b = \frac{0.1(h^2)}{1-h^2}$$

$$h = \sqrt{\frac{K_b}{0.1}}$$

$$[\text{OH}^-] = 0.1h = 0.1 \sqrt{\frac{K_b}{0.1}}$$

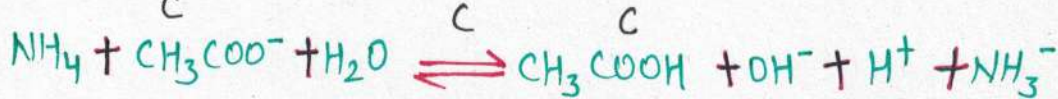
$$p^{\text{OH}} = -\frac{1}{2} (\log(0.1) + \log(10^{-14}) - \log K_a)$$

$$\begin{aligned}
 \text{pH} &= 7 + \frac{1}{2} \left(\frac{1 - 0.26}{+14} \right) \\
 &= 7 + \frac{15.26}{2} \\
 &= 7 + 1.87
 \end{aligned}$$

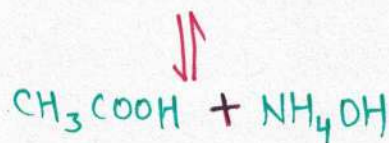
$$\boxed{\text{pH} = 8.87}$$

4.

Salt of Weak Acid + Weak Base

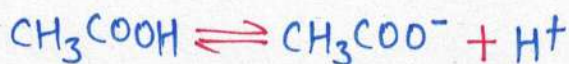
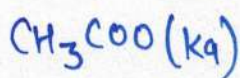


$$\begin{array}{l}
 f=0 \quad c \quad c \\
 f=f \quad c(1-h) \quad c(1-h)
 \end{array}$$

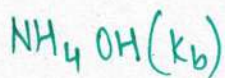


$$K_h = \frac{[\text{CH}_3\text{COOH}][\text{NH}_4\text{OH}]^{c_h}}{[\text{CH}_3\text{COO}^-][\text{NH}_4^+]} = \frac{chch}{c(1-h)c(1-h)}$$

$$\boxed{K_h = \left(\frac{h}{1-h} \right)^2}$$



$$K_a = \frac{[\text{CH}_3\text{COO}^-][\text{H}^+]}{[\text{CH}_3\text{COOH}]}$$



$$K_b = \frac{[\text{NH}_3][\text{OH}^-]}{[\text{NH}_4\text{OH}]}$$

$$K_a \cdot K_b = \frac{[\text{CH}_3\text{COO}^-][\text{H}^+]}{[\text{CH}_3\text{COOH}]} \cdot \frac{[\text{NH}_3][\text{OH}^-]}{[\text{NH}_4\text{OH}]}$$

$$K_a \cdot K_b = \frac{K_w}{K_h}$$

$$\boxed{K_h = \frac{K_w}{K_a \cdot K_b}}$$

$$\frac{h}{1-h} = \sqrt{K_h}$$

$$h = \sqrt{K_h} - h\sqrt{K_h}$$

$$h = \frac{\sqrt{K_h}}{1 + \sqrt{K_h}}$$

$$K_a = \frac{[\text{CH}_3\text{COO}^-][\text{H}^+]}{[\text{CH}_3\text{COOH}]}$$

$$K_a = \frac{h(1-h)[\text{H}^+]}{h}$$

$$[\text{H}^+] = \frac{h \cdot K_a}{1-h}$$

$$[\text{H}^+] = K_a \sqrt{\frac{K_w}{K_a K_b}} = \sqrt{\frac{K_a K_w}{K_b}}$$

$$\text{pH} = -\log [\text{H}^+] = -\frac{1}{2} (\log K_a + \log K_w - \log K_b)$$

$$\text{pH} = 7 + \frac{1}{2} (\text{p}K_a - \text{p}K_b)$$

1. if $K_a = K_b$ $\text{pH} = 7$ (Neutral Salt)
2. if $K_a > K_b$ $\text{p}K_a < \text{p}K_b$ $\text{pH} < 7$ (Acidic Salt)
3. if $K_a < K_b$ $\text{p}K_a > \text{p}K_b$ $\text{pH} > 7$ (Basic Salt)

In this case, K_h & pH are independent of the concentration.



BUFFER

SOLUTION

Solution having constant pH is called **buffer solution**.

It is of 2 kind:-

1. ACIDIC BUFFER


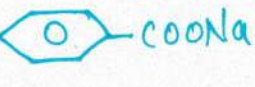
A solution having weak acid with its conjugate base in significant amount.


2. BASIC BUFFER

A solution having weak base with its conjugate acid in significant amount.

QUESTION

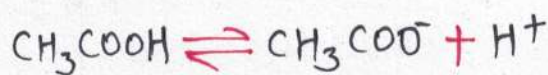
Identify buffer :-

- | | | | |
|---|---|-------------------------------------|---------------|
| 1 | $\text{CH}_3\text{COOH} / \text{CH}_3\text{COO}^-$ | <input checked="" type="checkbox"/> | Acidic buffer |
| 2 |  /  | <input checked="" type="checkbox"/> | Acidic buffer |
| 3 | $\text{NH}_3 / \text{NH}_4\text{Cl}$ | <input checked="" type="checkbox"/> | Basic buffer |
| 4 | $\text{CH}_3\text{NH}_2 / \text{CH}_3\text{NH}_3\text{Cl}$ | <input checked="" type="checkbox"/> | Basic buffer |
| 5 | HCl / Cl^- | <input type="checkbox"/> | Not buffer |
| 6 | $\text{H}_2\text{SO}_4 / \text{HSO}_4^-$ | <input type="checkbox"/> | Not buffer |
| 7 | $\text{H}_2\text{SO}_4 / \text{SO}_4^{2-}$ | <input type="checkbox"/> | Not buffer |
| 8 | $\text{H}_2\text{S} / \text{HS}^-$ | <input checked="" type="checkbox"/> | Acidic buffer |
| 9 | $\text{HS}^- / \text{S}^{2-}$ | <input checked="" type="checkbox"/> | Acidic buffer |

- | | | | |
|----|---|-------------------------------------|---------------|
| 10 | H_2S/S^{2-} | <input type="checkbox"/> | Not Buffer |
| 11 | H_2PO_4/HPO_4^{2-} | <input type="checkbox"/> | Not Buffer |
| 12 | $H_2PO_4^-/PO_4^{3-}$ | <input checked="" type="checkbox"/> | Acidic Buffer |
| 13 | $NH_2NH_2/NH_2NH_3^+ Cl^-$ | <input checked="" type="checkbox"/> | Basic Buffer |
| 14 | $NH_2NH_2/(NH_3NH_3^+) Cl^-$ | <input type="checkbox"/> | Not Buffer |
| 15 |  $NH_2NH_2 / NH_3NH_3^+$ | <input checked="" type="checkbox"/> | Basic buffer |

PH CALCULATION FOR ACIDIC BUFFER

Concentration :-	CH_3COO^-	CH_3COOH	
moles :-	c_1	c_2	$c_1 = \frac{a}{V}$
	a	b	$c_2 = \frac{b}{V}$



$t=0$	c_2	c_1	
$t=t$	$c_2 - x$	$c_1 + x$	x

$$K_a = \frac{(c_1 + x)(x)}{c_2 - x}$$

ignore x w.r.t. c_1 & c_2

$$K_a = \left(\frac{c_1}{c_2}\right)x$$

$$\left\{ x = [H^+] \Rightarrow -\log x = -\log [H^+] \right\}$$

= pH

$$-\log K_a = -\log \left(\frac{c_1}{c_2}\right) - \log x$$

$$pK_a = -\log \left(\frac{c_1}{c_2}\right) + pH$$

$$pH = pK_a + \log \left(\frac{c_1}{c_2} \right)$$

$$pH = pK_a + \log \frac{[\text{salt}]}{[\text{Acid}]} \rightarrow \text{Henderson's equation}$$

$$pH = -pK_a + \log \left[\frac{a}{b} \right] \rightarrow \text{Constant}$$

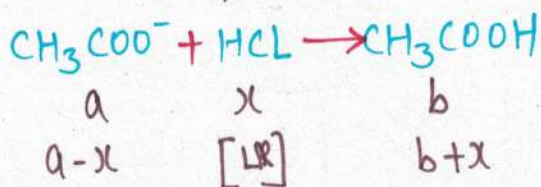


If H_2O is added

$$pH = pK_a + \log \left(\frac{a}{b} \right)$$



x mole HCl , $x \ll a, b$



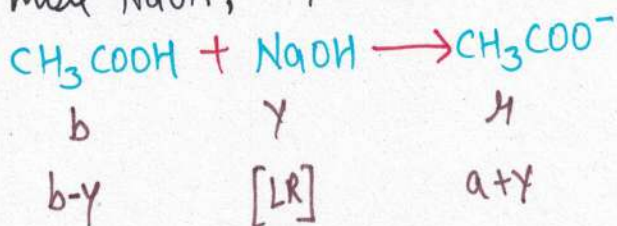
$$pH = pK_a + \log \left(\frac{b-x}{a+x} \right)$$

x is small

$$pH = pK_a + \log \left[\frac{b}{a} \right]$$



Y mole $NaOH$, $Y \ll a, b$



$$pH = pK_a + \log \left[\frac{a+Y}{b-Y} \right]$$

Y is small

$$pH = pK_a + \log \left(\frac{a}{b} \right) \rightarrow \text{Constant}$$

QUESTION

10 mole CH_3COOH is present with 10 mole CH_3COONa in 1L solution. what will be

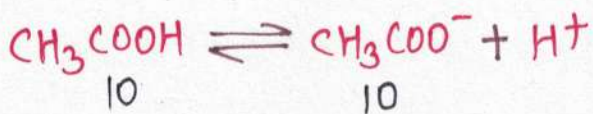
i) the pH of this solution

ii) if 2L water is added

iii) 2 mole NaOH added

iv) 2 mole KCl added

i)



$$\text{pH} = \text{pK}_a + \log\left(\frac{a}{b}\right)$$

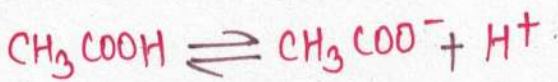
$$\text{pH} = -\log(1.8 \times 10^{-5}) + \log\left(\frac{10}{10}\right)$$

$$\text{pH} = -(0.26 - 5) + \log 1$$

$$\text{pH} = 5 - 0.26 = 4.74$$

ii)

If 2L water is added



$$\text{pH} = \text{pK}_a + \log\left[\frac{5}{5}\right]$$

$$\text{pH} = 4.74$$

$$[\text{acid}] = \frac{10}{2} = 5$$

$$[\text{Salt}] = 5$$

iii)

If 2 mole HCl is added



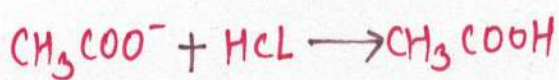
$$\begin{array}{ccc} 10 & 2 & \\ 10 - 2 = 8 & 0 & 10 + 2 = 12 \end{array}$$

$$\text{pH} = 4.74 + \log\left[\frac{12^3}{8^2}\right]$$

$$\text{pH} = 4.74 + 0.48 - 0.3$$

$$\text{pH} = 4.92$$

iv



$$\begin{array}{ccc} 10 & 2 & 10 \\ 8 & \text{LR} & 12 \end{array}$$

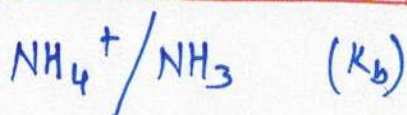
$$\text{pH} = 4.74 + \log\left(\frac{8}{12}\right)$$

$$\text{pH} = 4.74 + 0.3 - 0.48$$

$$\text{pH} = 4.56$$



PH CALCULATION FOR BASIC BUFFER

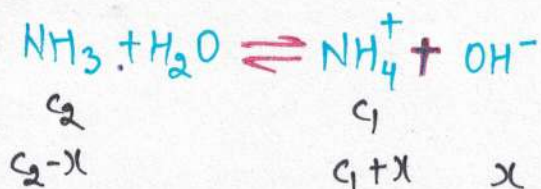


$$a \quad b$$

$$c_1 \quad c_2$$

$$c_1 = \frac{a}{V}$$

$$c_2 = \frac{b}{V}$$



$$[-\log x = \text{pOH}]$$

$$K_b = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]} = \left(\frac{c_1 + x}{c_2 - x}\right) x$$

$$-\log K_b = -\log \frac{c_1}{c_2} - \log x$$

$$\text{p}K_b = -\log \frac{c_1}{c_2} + \text{pOH}$$

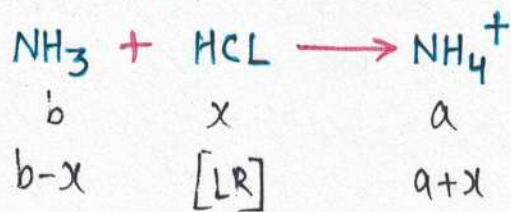
$$\text{pOH} = \text{p}K_b + \log \left[\frac{\text{salt}}{\text{Base}} \right]$$

$$\text{pOH} = \text{p}K_b + \log \left[\frac{a}{b} \right]$$



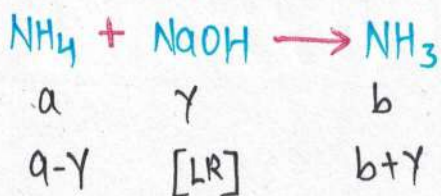
Dilution $\text{pH} = 14 - \text{pOH}$

2. x mole HCL is added.



$$pOH = pK_b + \log \left(\frac{a+x}{b-x} \right)$$

3. γ mole NaOH is added



$$pOH = pK_b + \log \left(\frac{a-\gamma}{b+\gamma} \right)$$



10 mole NH_3 is taken with 10 mole NH_4^+ in 1 lt soln. what will be the pH of soln

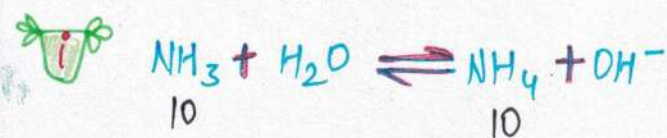
i. $K_b = 1.8 \times 10^{-5}$ of NH_3

ii. if 2lt H_2O is added

iii. if 2 mole HCL added

iv. 2 mole NaOH added

Solu:-



$$pOH = pK_b + \log \left(\frac{10}{10} \right)$$

$$pOH = -\log (1.8 \times 10^{-5})$$

$$pOH = 4.74$$

$$pH = 14 - 4.74 = 9.26$$

ii. No effect on delution

$$pH = 9.26$$





$$f \neq 0 \quad 10 \quad 2 \quad 10$$

$$f = f \quad 10-2 \quad 10+2$$

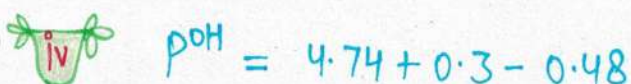
$$\quad \quad 8 \quad \quad 12$$

$$pOH = 4.74 + \log \frac{12}{8} - \frac{3}{2}$$

$$pOH = 4.74 + 0.48 - 0.3$$

$$pOH = 4.92$$

$$pOH = 14 - 4.92 = 9.08$$



$$= 5.04 - 0.48$$

$$= 4.56$$

$$pOH = 14.00 - 4.56$$

$$= 9.44$$

QUE What is pH?

i 500 ml 0.1 M CH_3COOH ($K_a = 10^{-5}$)



$$[\text{H}^+] = \sqrt{cK_a}$$

$$[\text{H}^+] = \sqrt{0.1 \times 10^{-5}}$$

$$[\text{H}^+] = \sqrt{10^{-6}}$$

$$[\text{H}^+] = 10^{-3}$$

$$pH = -\log(10^{-3}) = 3$$

ii 500 ml 0.1 M COOH + 100 ml 0.1 M NaOH



millimole	50	10	
	40	[LR]	10

This is a buffer solution

$$pH = pK_a + \log\left(\frac{10}{40}\right)$$

$$pH = -\log(10^{-5}) + \log\left(\frac{1}{4}\right)$$

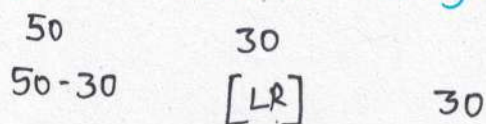
$$pH = 5 + 0 - 2(0.3)$$

$$pH = 5 - 0.6$$

$$pH = 4.4$$

iii

500 ml 0.1M CH_3COOH + 300 ml 0.1M $NaOH$



This is a buffer solution

$$pH = 5 + \log\left(\frac{30}{20}\right)$$

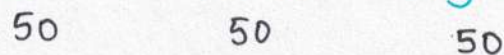
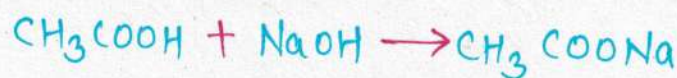
$$pH = 5 + \log 3 - \log 2$$

$$pH = 5 + 0.48 - 0.3$$

$$pH = 5.18$$

iv

500 ml 0.1M CH_3COOH + 500 ml 0.1M $NaOH$



$$[CH_3COONa] = \frac{50}{1000} = \frac{5}{100}$$

Salt hydrolysis

$$pH = 7 + \frac{1}{2} [\log C + pK_a]$$

$$pH = 7 + \frac{1}{2} [\log\left(\frac{5}{100}\right) + 5]$$

$$pH = 7 + \frac{1}{2} [0.7 - 2 + 5]$$

$$pH = 7 + \frac{1}{2} (3.7)$$

$$pH = 7 + 1.85$$

$$pH = 8.85$$

211

Y.

500 ml 0.1M CH₃COOH + 700 ml 0.1M NaOH



50	70	
[LR]	70 - 50	50
	= 20	

Weak base + strong base

[OH⁻] governed from strong base

[OH⁻] = 20 / 1200 = 1/60

pOH = -log(1/60) = log 60 = log 2 + log 3 + 1
 = 0.3 + 0.48 + 1
 = 1.78

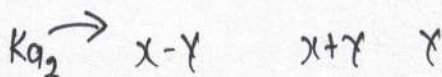
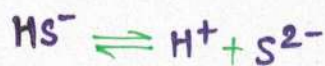
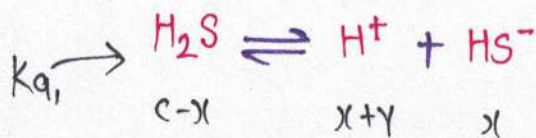
pH = 14 - 1.78

pH = 12.26

WEAK POLYPROTIC ACID



K_{a1} >> K_{a2}



We can ignore
 x w.r.t c
 y w.r.t x

K_{a1} = $\frac{[H^+][HS^-]}{[H_2S]}$ = $\frac{(x+y)(x)}{c-x}$

K_{a1} >> K_{a2}

K_{a1} = $\frac{x^2}{c}$

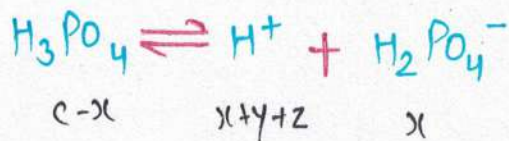
x = $\frac{c}{\sqrt{cK_{a1}}}$

$[H^+]$ will be governed from 1st step

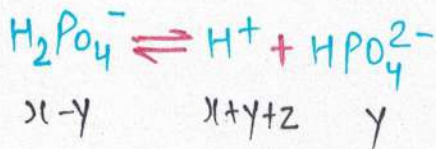
$$K_{a2} = \frac{[H^+][S^{2-}]}{[HS^-]} = \frac{(x+y)(y)}{(x-y)^0} = \gamma$$

$$\gamma = K_{a2} = [S^{2-}]$$

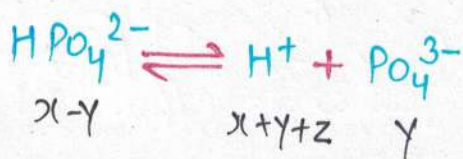
$$\alpha_{H_2S} = \frac{x}{c} \quad \therefore \alpha_{H_2S} = 0.1$$



$$K_{a1} = \frac{(x+y+z)x}{c-x} = \frac{x^2}{c}$$

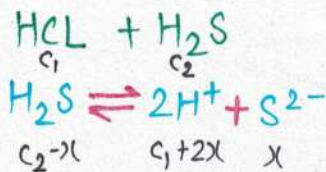


$$K_{a2} = \frac{(x+y+z)y}{x-y} \approx \gamma = K_{a2}$$



$$K_{a3} = \frac{(x+y+z)z}{y-z} \approx \frac{xz}{y} = K_{a3}$$

where H^+ is governed from strong acid (outside).

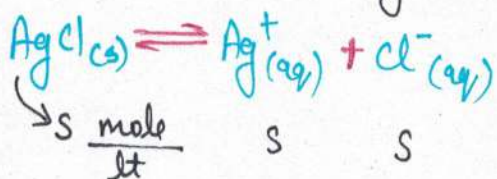


$$K_a = K_{a1} \cdot K_{a2} = \frac{[H^+]^2 [S^{2-}]}{[H_2S]}$$

$K_{a1}, K_{a2}, [H^+], [H_2S]$ will be given $[S^{2-}]$ can be calculated.

SOLUBILITY AND SOLUBILITY PRODUCT

In this section, we'll study about sparingly soluble salts.



$$K_{sp} = [\text{Ag}^+][\text{Cl}^-] = s \cdot s = s^2$$

$$s = \sqrt{K_{sp}}$$

K_{sp} = solubility product

K_{sp} only depend on temperature.

on addition of solid at a particular temperature will have no effect on solubility.

solvent \rightarrow H_2O



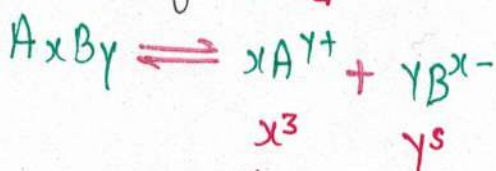
$$K_{sp} = [\text{Pb}^{+2}][\text{Cl}^-]^2 = s \cdot (2s)^2 = 4s^3$$

$$s^3 = \frac{K_{sp}}{4}$$

$$s = \left(\frac{K_{sp}}{4}\right)^{1/3}$$

s is solubility of PbCl_2

Generalise



$$K_{sp} = (xs)^x (ys)^y = x^y y^x s^{x+y}$$





$$K_{sp} = (3s)^3(s)$$

$$K_{sp} = 27s^4$$



Ionic product $\text{I.P} = [\text{Ag}^+][\text{Cl}^-]$

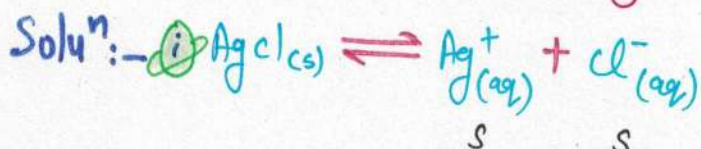
- if $\text{I.P} = K_{sp}$ saturated solution
 $\text{I.P} < K_{sp}$ unsaturated solution
 $\text{I.P} > K_{sp}$ supersaturated solution
 (ppt occur)

Remember $Q_c, K_c!!$

SOLUBILITY IN COMMON ION

QUE. AgCl ($K_{sp} = 10^{-10}$)

- i) What will be solubility in water
- ii) what will be solubility in 0.1M KCl soln
- iii) what will be solubility in 0.1M AgNO_3 soln

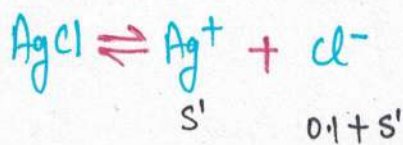
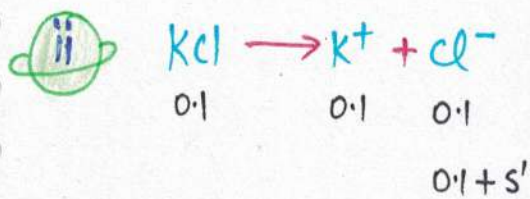


$$K_{sp} = s^2$$

$$s = \sqrt{K_{sp}}$$

$$= \sqrt{10^{-10}}$$

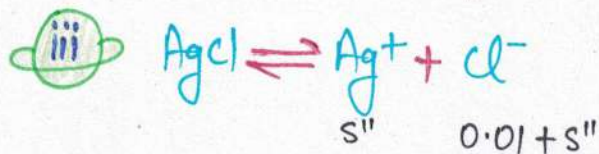
$$= 10^{-5}$$



$$K_{sp} = s'(0.1 + s')$$

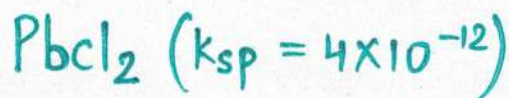
$$10^{-10} = 10^{-1} s'$$

$$s' = 10^{-9} \text{ mol/lit}$$



$$10^{-10} = 10^{-2} s''$$

$$s'' = 10^{-8} \text{ mol/lit}$$



What will be solubility

i) in H_2O

ii) in 0.01M HCl

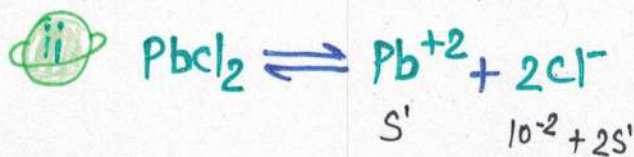
iii) in 0.01M $Pb(NO_3)_2$



$$K_{sp} = s \cdot (2s)^2$$

$$\frac{4 \times 10^{-12}}{4} = s^3$$

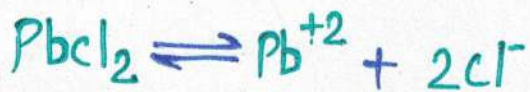
$$s = 10^{-4} \text{ mol/lit}$$



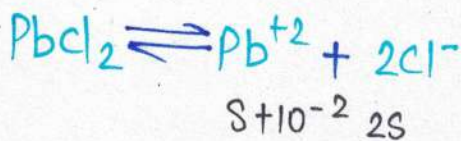
$$K_{sp} = (10^{-2} + 2s')^2 s'$$

$$\frac{4 \times 10^{-12}}{10^{-2}} = s'$$

$$s' = 4 \times 10^{-8}$$



$$4 \times 10^{-12} = s'' (10^{-2} + 2s'')^2$$



$$4 \times 10^{-12} = (s + 10^{-2})(2s)^2$$

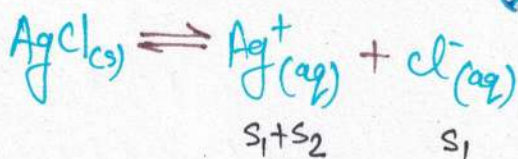
$$4 \times 10^{-12} = 10^{-2} \times 4s^2$$

$$10^{-10} = s^2$$

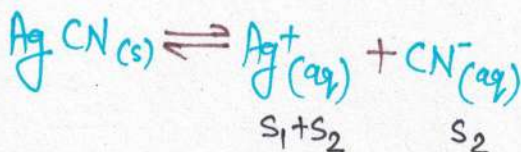
$$s = 10^{-5}$$

Here, solubility is decreasing due to common ion.

SIMULTANEOUS SOLUBILITY



$$K_{sp1} = (s_1 + s_2)s_1$$



$$K_{sp2} = (s_1 + s_2)s_2$$

$$K_{sp1} + K_{sp2} = (s_1 + s_2)(s_1 + s_2)$$

$$= (s_1 + s_2)^2$$

$$s_1 + s_2 = \sqrt{K_{sp1} + K_{sp2}}$$



SELECTIVE - PRECIPITATION

QUE

In a solution $[I^-] = [Br^-] = [Cl^-] = 0.01M$

$AgNO_3$ is added slowly.

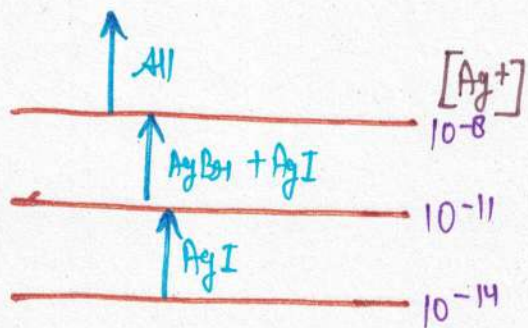
- i) Which ion will precipitate first?
- ii) What will be % precipitation of first ion, when 2nd will start precipitating?
- iii) What will be % precipitation of other ions when last ion will start precipitating.

(Given :- K_{sp} of $AgCl = 10^{-10}$, K_{sp} of $AgBr = 10^{-13}$
 K_{sp} of $AgI \rightarrow 10^{-16}$)

Soluⁿ:- for $AgCl$ $[Ag^+][Cl^-] = K_{sp}$
 $[Ag^+] = \frac{10^{-10}}{10^{-2}} = 10^{-8}$

for $AgBr$ $[Ag^+][Br^-] = 10^{-13}$
 $[Ag^+] = \frac{10^{-13}}{10^{-2}} = 10^{-11}$

for AgI $[Ag^+][I^-] = 10^{-16}$
 $[Ag^+] = \frac{10^{-16}}{10^{-2}} = 10^{-14}$



i) AgI will precipitate first.

iii) When $AgBr$ will start precipitating.
 $[Ag^+] = 10^{-11}$

$$\text{for AgI} = [\text{Ag}^+][\text{I}^-] = 10^{-16}$$

$$[\text{I}^-] = \frac{10^{-16}}{10^{-11}} = 10^{-5}$$

$$\% \text{ remain} = \frac{10^{-5}}{10^{-2}} \times 100 = 0.1\%$$

$$\begin{aligned} \% \text{ ppt} &= 100 - 0.1 \\ &= 99.9\% \end{aligned}$$



$$[\text{Ag}^+] = 10^{-8}$$

for AgI

$$[\text{Ag}^+][\text{I}^-] = 10^{-16}$$

$$[\text{I}^-] = \frac{10^{-16}}{10^{-8}} = 10^{-8}$$

$$\% \text{ remain} = \frac{10^{-8}}{10^{-2}} \times 100 = 10^{-4}\%$$

$$\begin{aligned} \% \text{ ppt} &= 100 - 0.0001 \\ &= 99.9999\% \end{aligned}$$

for AgBy

$$[\text{Ag}^+][\text{By}^-] = 10^{-13}$$

$$[\text{By}^-] = \frac{10^{-13}}{10^{-8}} = 10^{-5}$$

$$\% \text{ remain} = \frac{10^{-5}}{10^{-2}} \times 100 = 10^{-1}\%$$

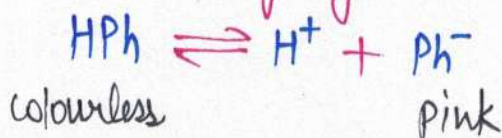
$$\begin{aligned} \% \text{ ppt} &= 100 - 0.1 = 99.9\% \end{aligned}$$



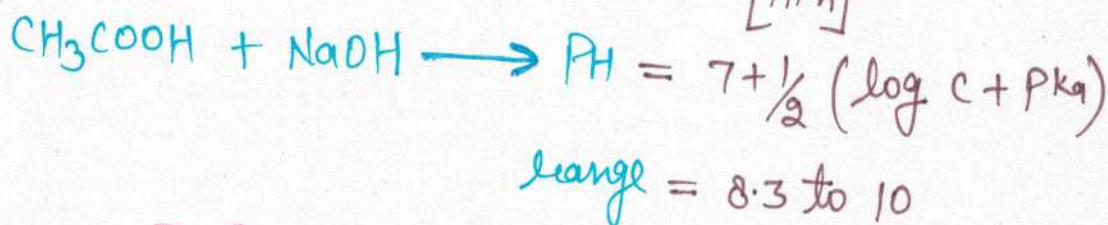
THEORY OF INDICATORS

Indicators are organic substances which have different colours in ionised and unionised form.

phenolphthalein :- slightly basic medium



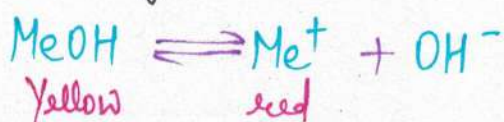
$$K_a = \frac{[\text{H}^+][\text{Ph}^-]}{[\text{HPh}]} \Rightarrow -\log K_a = -\log [\text{H}^+] - \log \frac{[\text{Ph}^-]}{[\text{HPh}]}$$



$$\frac{[\text{Ph}^-]}{[\text{HPh}]} \geq 10 \quad \text{pink}$$

$$\frac{[\text{Ph}^-]}{[\text{HPh}]} \leq 10 \quad \text{colourless}$$

Methylene orange :- Acidic medium



eg:- NH_4Cl

$$\text{PH} = 7 - \frac{1}{2} (\log c + pK_b)$$

$$K_b = \frac{[Me^+][OH^-]}{[MeOH]}$$

$$p^{OH} = pK_b + \log \frac{[Me^+]}{[MeOH]}$$

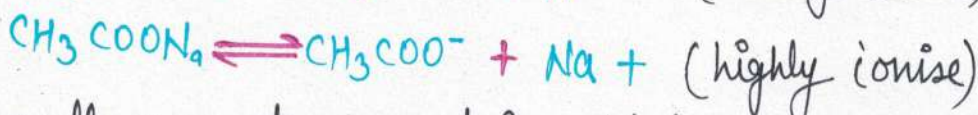
$$p^{OH} = pK_b + 1$$

pH range :- 3 to 5

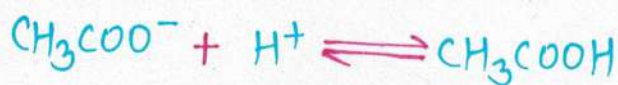
if $\frac{[Me^+]}{[MeOH]} \geq 10$ red

$\frac{[Me^+]}{[MeOH]} \leq 10$ Yellow

BETTER ACTION



➤ If small amount of acid is added in above buffer the following reaction will occur :-



$$K_a' = \frac{1}{K_a} = 10^5$$

Hence the added HCl will be almost completely furnished and pH change would not occur.

as $(K_a > 10^3)$

➤ If small amount of base is added in above buffer then



Hence the added base will be alive finished & pH change would not occur.

$$\frac{1}{K_H} = \frac{K_a}{K_w} = \frac{10^{-5}}{10^{-14}} = 10^9$$

PH of ACIDIC BUFFER

(as $K_a > 10^{-3}$)

$$pH = pK_a + \log \left[\frac{\text{salt}}{\text{acid}} \right]$$

$$pH = pK_a + \log \left[\frac{\text{conjugate base}}{\text{acid}} \right]$$

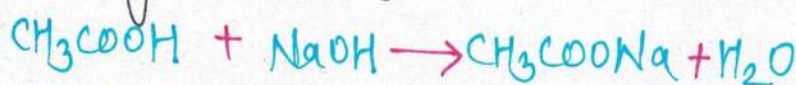


PH = ?

a. 0.1M CH_3COOH + 0.1M CH_3COONa ($pK_a = 4.74$)

$$pH = pK_a + \log \left(\frac{0.1}{0.1} \right)$$

b. equal volume of 0.1M CH_3COOH + 0.05M $NaOH$



$$t=t \quad 0.1V \quad .005V$$

$$t=0 \quad 0.10V - 0.05V \quad 0 \quad 0.05V$$

$$0.05V \quad 0.05V$$

$$pH = pK_a + \log \left(\frac{0.05V}{0.05V} \right) = 4.74$$

Range of Buffer: - $\frac{1}{10} \leq \left[\frac{CH_3COONa}{CH_3COOH} \right] \leq 10$

i.e.:- $pK_a - 1$ to $pK_a + 1$

By using an acidic Buffer, solⁿ of pH from $pK_a - 1$ to $pK_a + 1$ can be formed.

★ In any type of 2 solutions mixtures.

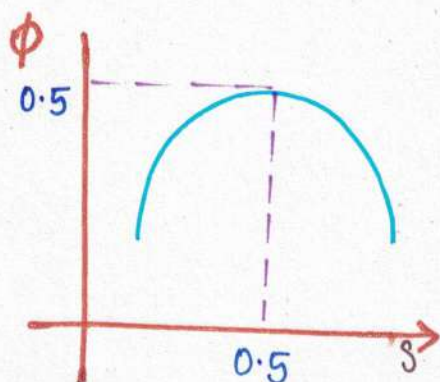
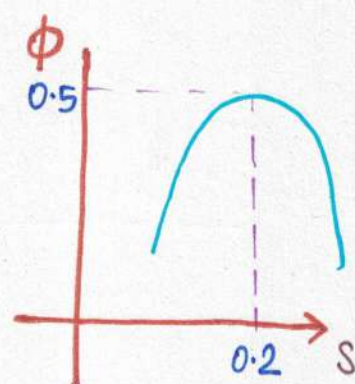
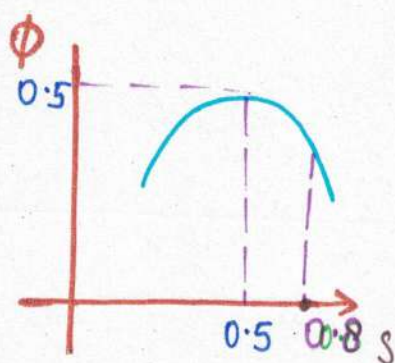
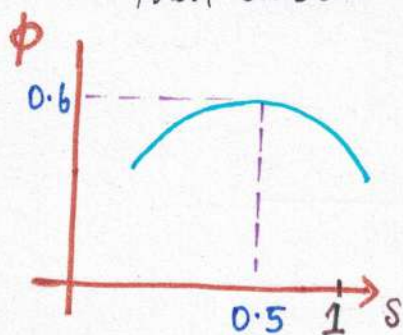
★ pH difference b/w them is 1, then pH of resulting mixture will be = lower solutions $pH + 0.26$

★ pH difference is 2, then pH of resulting solⁿ = lower $pH + 0.29$

★ pH difference > 2 , then pH of resulting solⁿ = Lower $pH + 0.3$



In an acidic buffer, acid (a) and salt (s) has $a+s=1$. If a graph of buffer capacity will be salt amount is plotted then correct curve.



$$\therefore \left[\phi = 2.303 \frac{as}{a+s} = 2.303 \frac{0.25}{1} = 0.57575 \right]$$

INDICATORS AND TITRATIONS

Solutions which are used to detect the end point (equivalence pt) in acid base titration.

Indicator	pH range	colour change
Methyle orange	→ 3.2 - 4.5 →	Yellow to orange
Methyle red	→ 4.4 - 6.5 →	Yellow to red
Litmus	→ 5.5 - 7.5 →	red to blue

phenol red \rightarrow 6.8 - 8.4 \rightarrow red to yellow

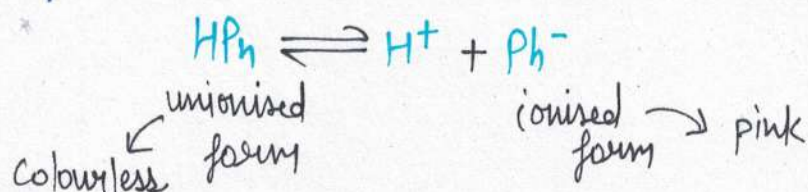
Phenolphthalein \rightarrow 8.3 - 10.5 \rightarrow colourless to pink

1.

OSTIVALD THEORY

Indicators are solⁿ of weak acid or weak base which will ionise less in one medium than in other. Both ionised and unionised forms have different colours.

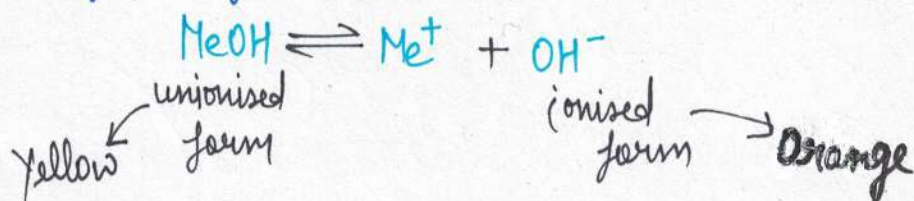
▷ Phenolphthalein is a weak acid which ionise as



In acidic medium HPh is colourless

In Basic medium HPh is pink

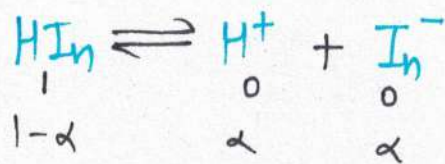
▷ Methyl orange is a weak base which ionise as



In acidic medium Me(OH) is orange

In Basic medium Me(OH) is yellow

▷ usually one form which is present in large percentage (>50%) will show its colour. But according to human eye sensitivity, one form is 10 times higher than the other, then the solution will show its colour.



$$\left[\frac{\text{In}^-}{\text{HIn}} \right] > 10 \quad (\text{colour of In}^- \text{ will be there})$$

$$\frac{\alpha}{1-\alpha} \geq 10$$

$$11\alpha \geq 10$$

$$\alpha \Rightarrow \frac{10}{11}$$

$$\alpha \geq 0.91$$

$$\% \text{ ionisation} \geq 91\%$$

$$\left[\frac{\text{In}^-}{\text{HIn}} \right] \leq \frac{1}{10} \quad (\text{colour of HIn will be there})$$

$$\frac{\alpha}{1-\alpha} \leq \frac{1}{10}$$

$$\alpha \leq \frac{1}{11}$$

$$\alpha \leq 0.091$$

$$\% \text{ ionisation} \leq 9.1\%$$

PH OF INDICATOR SOLUTION

Solution of indicator will act as buffer.

Hence

$$\text{PH of acid indicator} \quad \text{pH} = \text{pK}_a + \log \left[\frac{\text{In}^-}{\text{HIn}} \right]$$

$$\text{or.} \quad \text{pH} = \text{pK}_a + \log \left[\frac{\alpha}{1-\alpha} \right]$$

$$\text{PH of basic indicator} \quad \text{pH} = \text{pK}_a + \log \left[\frac{\text{conj. acid}}{\text{base}} \right]$$

QUE. Calculate the pH of acid indicator solⁿ which ionise to 30% in solution ($pK_{In} = 4.7$)

Solⁿ:- $pH = pK_a + \log \left(\frac{\alpha}{1-\alpha} \right)$
 $pH = 4.7 + \log \left(\frac{0.3}{0.7} \right)$

$$\alpha = 0.3$$

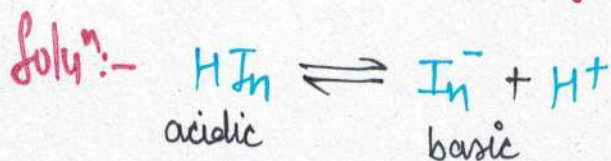
$$pK_a = 4.7$$

$$4.7 + 0.48 - 1$$

$$= 5.18 - 0.84 = 4.34$$

$$pK_a = 4.34$$

QUE. An Acid indicator show (blue) colour in acidic form and red in basic form. Blue colour will appear only when acidic form is 10 times higher than basic form and red colour will appear only when basic form is 5 times greater than acidic form. What will be pH range of indicator? ($pK_{In} = 5$)



Blue colour $pH = pK_a + \log \left[\frac{In^-}{HIn} \right]$
 $pH = 5 + \log \left(\frac{1}{10} \right)$
 $pH = 5 - 1 = 4$

$$\left[\frac{HIn}{In^-} \right] > 10$$

$$\boxed{pH = 4}$$

Red colour $pH = 5 + \log 5$
 $pH = 5 + 0.699$
 $pH = 5.699$

$$\left[\frac{In^-}{HIn} \right] > 5$$

$$\boxed{pH = 5.699}$$

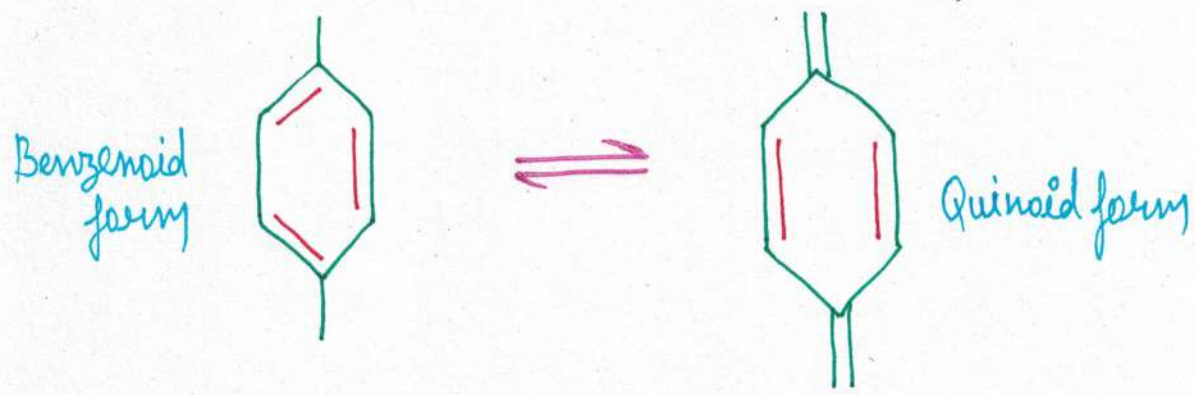
pH of indicator is of range 4 to 5.699 in the Question.

2.

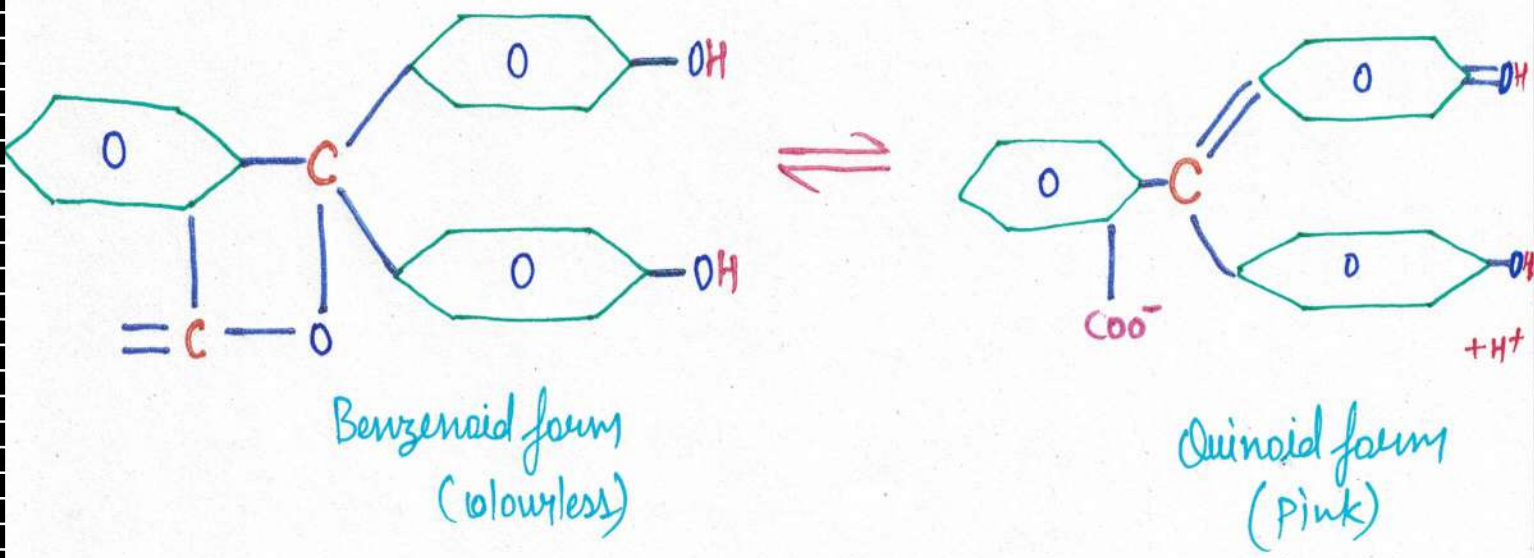
QUINOID THEORY

Indicators are solⁿ of weak organic acid or weak organic base.

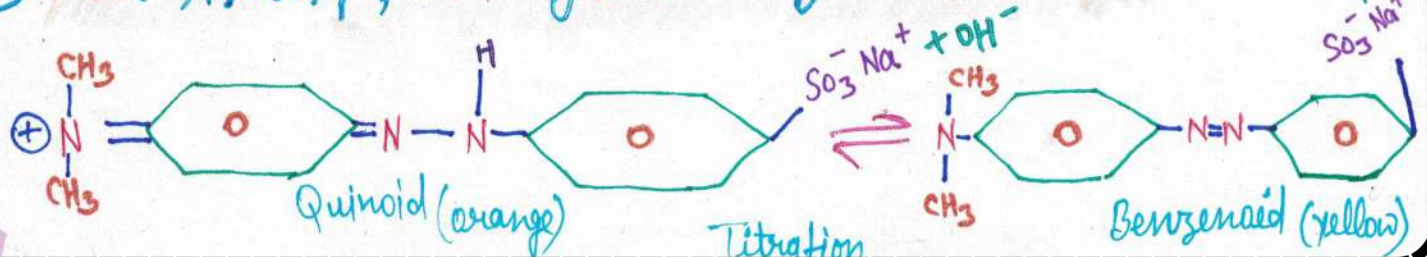
Indicators exist in the solⁿ either in quinoid form or in benzenoid form in which quinoid form is dark in colour.



Phenolphthalein indicator



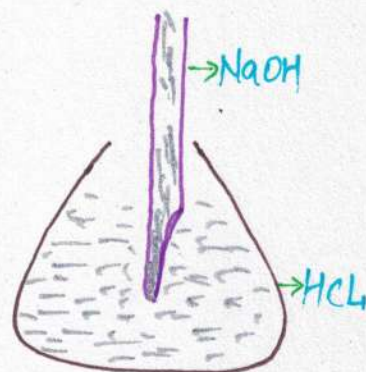
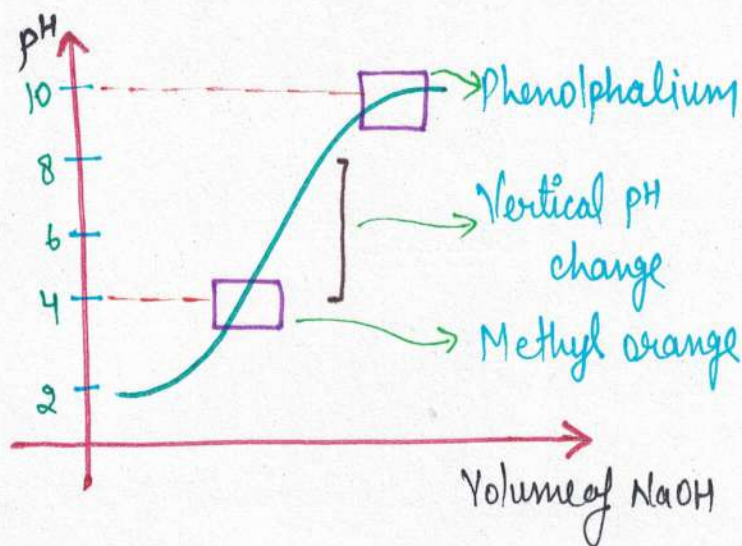
Similarly, methyl orange indicator



- ▶ The process in which end point is detected by using an indicator.
- ▶ Selection of indicator is based on a vertical pH change in a titration.



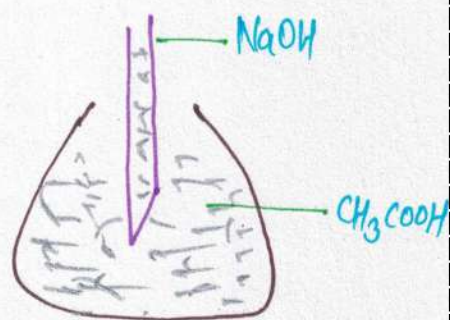
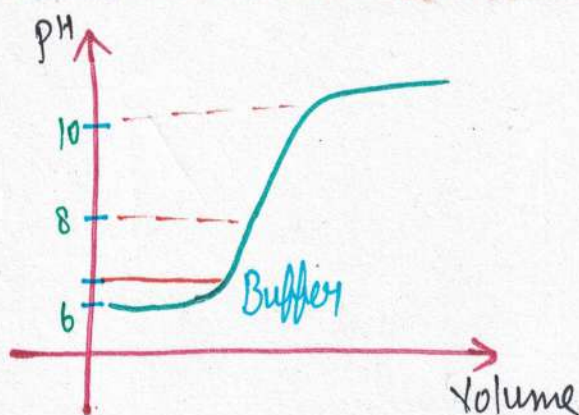
Titration of a Strong Acid and strong Base



Vertical pH change is from 4 to 10



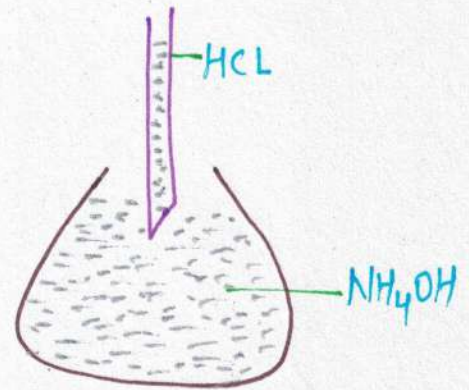
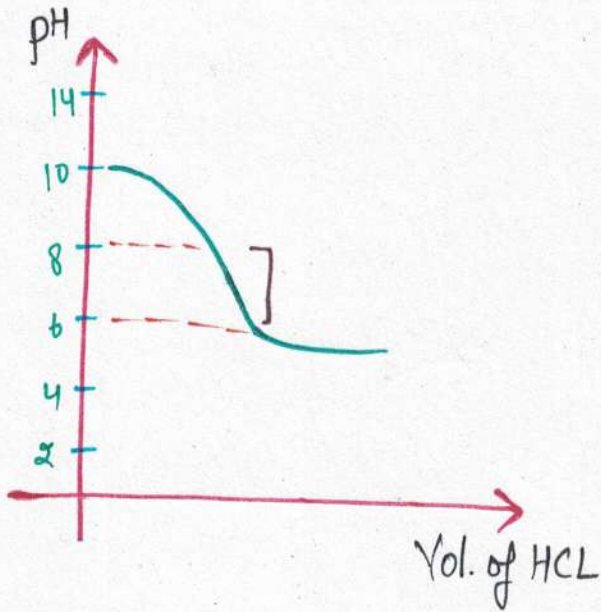
Titration of Weak Acid with Strong Base



Vertical pH change is from 7 to 10



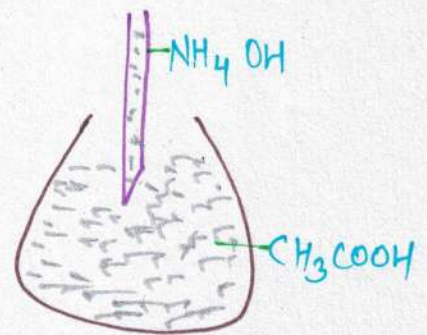
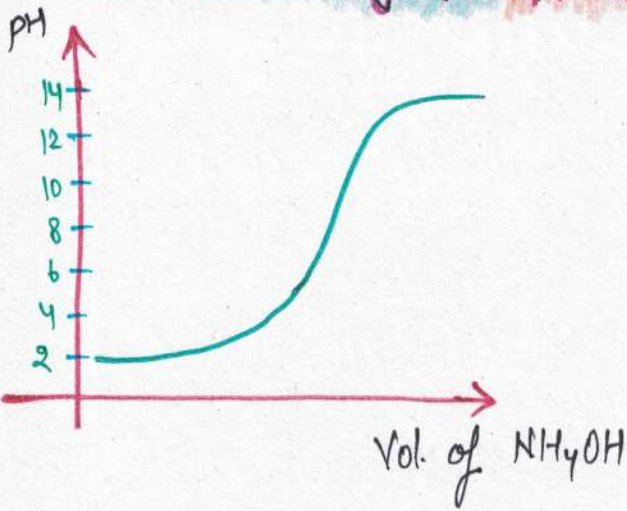
Titration of Weak base and strong acid



Vertical pH change is from 10 to 7



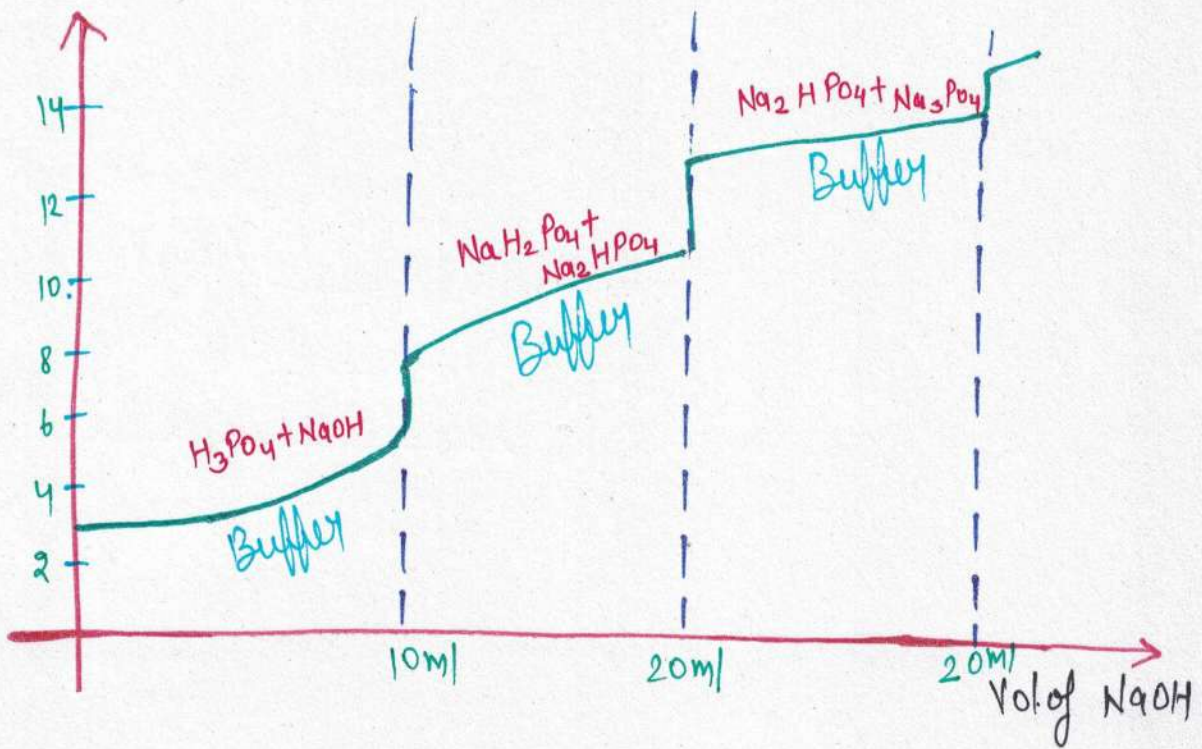
Titration of Weak acid and Weak base



No Vertical pH change here



Titration of Weak Polyprotic acid and strong base

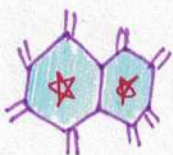


No. of Buffer formed will depend on polyprotic index of weak acid.

IONIC EQUILIBRIUM

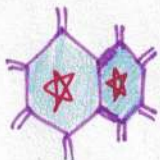
SHORT

NOTES



"P" operator take $(-\log)$ of the variables.

eg:- $\text{pH} = -\log(\text{H}^+)$ $\text{pK}_a = -\log(\text{K}_a)$



At 25°C , the $\text{K}_w = 10^{-14}$



$$\text{K}_w = [\text{H}^+][\text{OH}^-] = 10^{-14} \quad \text{--- (1)}$$

Taking $-\log$ on both side of (1)

$$\text{pH} + \text{pOH} = 14$$

$\text{pH} = 7 \rightarrow$ Neutral

$\text{pH} < 7 \rightarrow$ Acidic

$\text{pH} > 7 \rightarrow$ Basic



pH Calculation:- $pH = -\log [H^+] = -\log \left(\frac{\text{moles of } H^+}{\text{Volume}} \right)$

e.g:- 300ml of 0.1M HCL

millimoles of $(H^+) = 0.1 \times 300 = 30$, Volume = 300

$$pH = -\log \left(\frac{30}{300} \right) = -\log (10^{-1}) = 1$$



For strong acids:- Calculate pH of 300ml 0.3M H_2SO_4

millimoles of $H^+ = 300 \times 0.3 \times 2 = 180$

Volume = 300ml ↓
2 H^+ present

$$\therefore [H^+] = \frac{180}{300}, \quad pH = -\log \left(\frac{180}{300} \right)$$



pH calculation for weak Acid:-



t=0 c

t=t 1- α c α c α

$$K_a = \frac{c\alpha^2}{1-\alpha} \Rightarrow \alpha = \sqrt{\frac{K_a}{c}} \Rightarrow [H^+] = c\alpha = \sqrt{K_a c}$$

$$pH = -\log(\sqrt{K_a c})$$

$$pH = \frac{1}{2}(-\log c + pK_a)$$



pH Calculation for (strong + weak) Acid

- ▶ Here, pH will be governed by the strong acid only.
- ▶ Thus, only take $[H^+]$ of strong acid as the $[H^+]$ of the weak acid will be ignored.

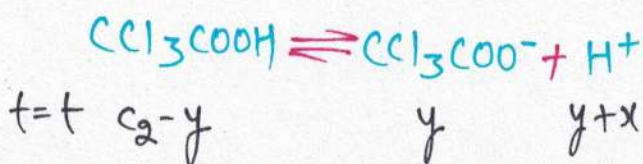
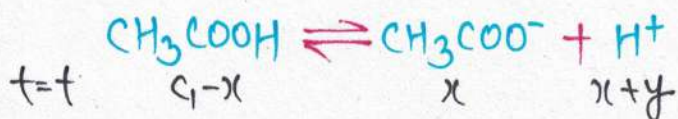
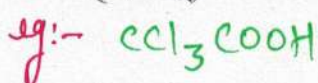
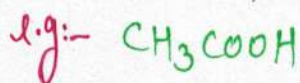
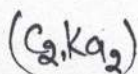
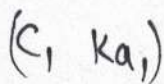


pH Calculation for (strong + weak) Base

▷ Here, pH will be governed by the strong base only as the [OH] coming from weak base can be ignored.



Weak acid + Weak acid



$$x + y = [H^+] = \sqrt{C_1 K_{a1} + C_2 K_{a2}}$$

$$pH = -\log(x + y)$$

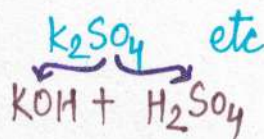
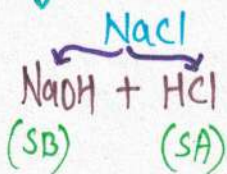


Salt hydrolysis

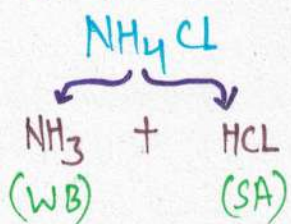
SA = Strong acid
WA = Weak acid



a. Salt of SA + SB

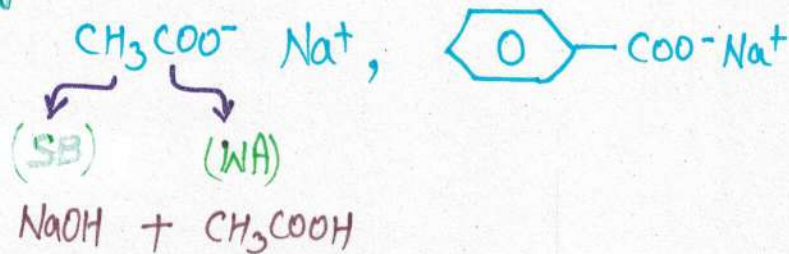


b. Salt of SA + WB

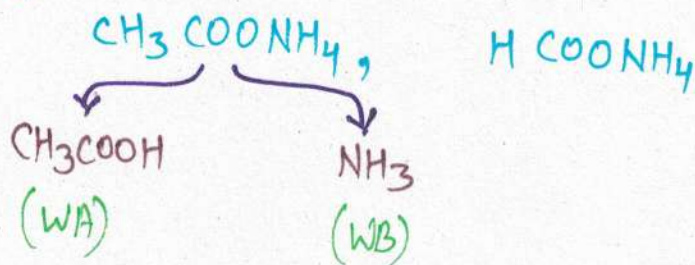




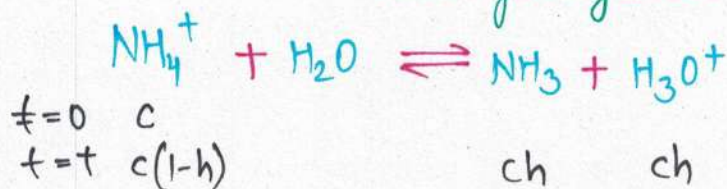
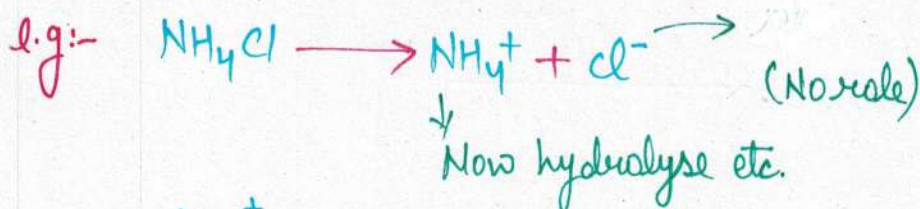
Salts of SB + WA



Salts of WA + WB



Here, instead of K_w, K_a, K_b ; we need to use K_h (hydrolysis) as to get the correct answer.



$$K_h = \frac{(ch)^2}{c(1-h)} = (ch)^2 \Rightarrow$$

$$h = \sqrt{\frac{K_h}{c}}$$

$$K_h = \frac{K_w}{K_b} \rightarrow \text{In Case of base}$$

$$K_h = \frac{K_w}{K_a} \rightarrow \text{In Case of acid}$$

$$\text{pH} = 7 - \frac{1}{2} (\log K_c + \text{p}K_b)$$

★ In Case of Salts of **WB + SA**

$$pH = 7 - \frac{1}{2} (\log C + pK_b)$$

★ In Case of salts of **WA + SB**

$$pH = 7 + \frac{1}{2} (\log C + pK_a)$$

★ Salts of weak acid + weak base

$$K_h = \left(\frac{h}{1-h}\right)^2 \quad K_h = \left(\frac{K_w}{K_a \cdot K_b}\right)$$

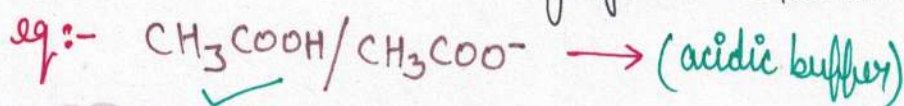
$$pH = 7 - \frac{1}{2} (pK_a - pK_b)$$



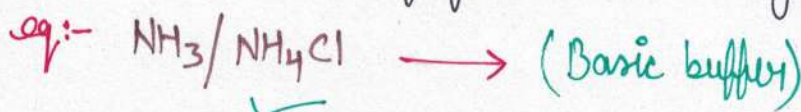
Buffer Solution

A solution having constant pH is called a buffer solution.

(i) **Acidic buffer** :- A solution having weak acid along with the conjugate base in significant amount.



(ii) **Basic buffer** :- A solution having weak base along with the conjugate acid in significant amount



pH Calculations for acidic buffer

$$pH = pK_a + \log \left(\frac{[\text{salt}]}{[\text{Acid}]} \right)$$



pH Calculations for basic buffer

$$pOH = pK_b + \log \left(\frac{[\text{salt}]}{[\text{Base}]} \right)$$

$$pH + pOH = 14$$



Weak polyprotic acid (H_3PO_4)



$$K_{a1} \quad t=t \quad c-x \quad x \quad x+y+z$$



$$K_{a2} \quad t=t \quad x-y \quad y \quad y+x+z$$



$$K_{a3} \quad t=t \quad y-z \quad z \quad z+x+y$$

$$K_{a1} = \frac{(x+y+z)(x)}{(c-x)} = \frac{x^2}{c}$$

$$K_{a2} = \frac{(x+y+z)(y)}{x-y}$$

①

$$K_{a2} = y \quad \text{--- ②}$$

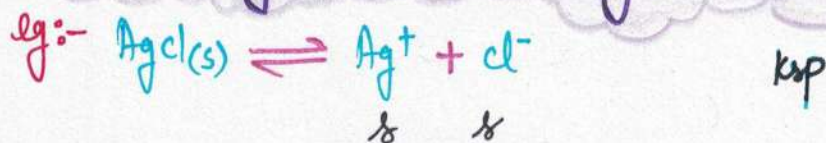
$$K_{a3} = \frac{(x+y+z)(z)}{(y-z)} = \frac{xz}{y} \quad \text{--- ③}$$

Calculate x, y, z from ① ② ③; and

$$[H^+] = x+y+z \quad \text{then} \quad pH = -\log(x+y+z)$$



Solubility and Solubility prod



$$K_{sp} = s^2$$



$$K_{sp} = (s)(2s)^2 = 4s^3$$